On a Logic for Coalitional Games with Priced-Resource Agents

D. Della Monica, M. Napoli, M. Parente

University of Salerno ddellamonica@unisa.it

LAMAS 2011 11th November, 2011 Osuna, Spain



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11/11/11 - 11h



At a glance

- We present the logic PRB-ATL
- PRB-ATL is inspired to existing extensions of ATL
 - ▶ To deal with bounded resources scenarios in multi-agent systems
- We studied the model checking for PRB-ATL
 - It is in EXPTIME (upper bound)
 - It is PSPACE-hard (lower bound)
- We studied the optimal coalition problem

Outline

- Introduction to Multi-Agent Systems (MAS) ATL
 - Multi-Agent Systems and resource constraints RB-ATL
- Our proposal: the logic Priced RB-ATL PRB-ATL
 - Model checking
 - Optimization problem
- 3 Conclusions



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- Several agents
- Intelligent (take decision)
- Independent
- Global state: union of single states
- Move choices
- Next state

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Agents and coalitions

COALITION - modeling collective behaviors/strategies

 Agents/Players can join in coalitions/teams to collectively perform tasks/reach goals

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> Two sides of the same coin Artificial Intelligence/Game theory

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Logical Formalisms

Coalition Logic (CL) and Alternating-time Temporal Logic (ATL)



CL and ATL

CL [Pauly, Journal of Logic and Computation, 2002]

ATL [Alur, Henzinger, Kupferman, Journal of ACM, 2002]

Theorem (Goranko, TARK 2001)

CL can be embedded into ATL

ATL: syntax and semantics

Formulae of ATL are given by the grammar:

$$\varphi ::= p \mid \neg \varphi \mid \varphi \land \varphi \mid \langle \langle A \rangle \rangle \bigcirc \varphi \mid \langle \langle A \rangle \rangle \varphi \mathcal{U} \varphi \mid \langle \langle A \rangle \rangle \Box \varphi$$

Formulae of ATL predicate about abilities of coalitions of agents

ATL: syntax and semantics

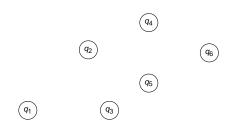
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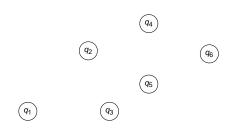
Formulae of ATL are evaluated wrt:

- a game structure (or game arena) G
- a location q of G

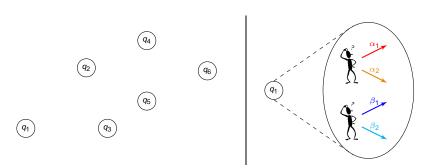


- locations labeled by atomic propositions
- in each location, each agent can choose among a non-empty set of actions
- any possible combination of actions gives rise to transitions (edges of the graph)



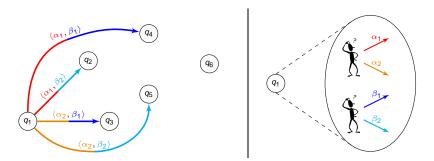


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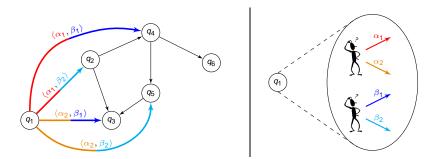


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Collective strategy to guarantee p holds

 $\langle\langle A \rangle\rangle \bigcirc p$ next $\langle\langle A \rangle\rangle \Box p$ always $\langle\langle A \rangle\rangle p \mathcal{U} q$ until q

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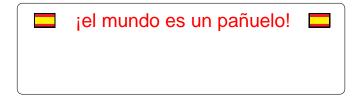
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regardless of actions performed by other agents (opponent)

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¡el mundo es un pañuelo!





It's a small world!







lt's a small world!



Quant'è piccolo il mondo!





¡el mundo es un pañuelo!



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Quant'è piccolo il mondo!



Resources are bounded

Extensions of ATL with bounds on resources

$$\langle\langle A^{\eta}\rangle\rangle\Box p$$

Endowment: $\eta: A \to \mathbb{N}^r$



The literature about Resource Bounded ATL (RB-ATL)

RB-ATL [Alechina, Logan, Nga, Rakib, AAMAS 2010]

Theorem: Model checking RB-ATL is decidable in $O(|\varphi|^{2\cdot r+1} \times |G|)$

No lower bound

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No lower bound

RAL [Bulling, Farwer, ECAI 2010]

If actions may produce resources, then Model Checking becomes UNDECIDABLE

RB-ATL: syntax and semantics

Formulae of RB-ATL are given by the grammar:

$$\varphi ::= p \mid \neg \varphi \mid \varphi \wedge \varphi \mid \langle \langle A^{\eta} \rangle \rangle \bigcirc \varphi \mid \langle \langle A^{\eta} \rangle \rangle \varphi \mathcal{U} \varphi \mid \langle \langle A^{\eta} \rangle \rangle \Box \varphi$$

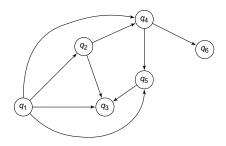
Formulae of RB-ATL predicate about abilities of coalitions whose agents are equipped with a finite endowment of resources

Formulae of RB-ATL are evaluated wrt:

- a resource-bounded game structure (or game arena) G
- a location q of G

The arena of RB-ATL

A resource-bounded game structure G is a weighted state transition graph:

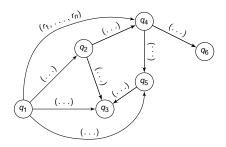


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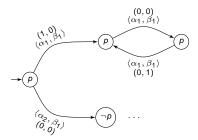
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An anomalous behavior

2 agents: **ag**₁ and **ag**₂ 1 resource type: **r**₁

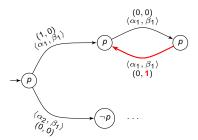
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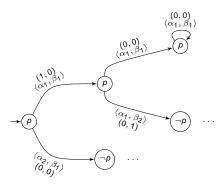
opponent consumes an infinite amount of resources



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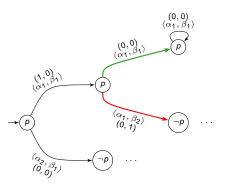
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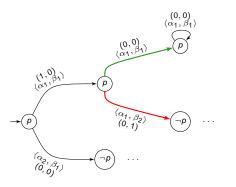


false if $r_1 > 1$ true if $r_1 = 1$

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opponent's moves should be constrained

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Weaknesses of previous approaches

- NO history (resources)
 - $G, q \Vdash \langle \langle A^{\eta} \rangle \rangle \bigcirc \langle \langle A^{\eta'} \rangle \rangle \Box p$

 η and η' are independent

- opponent does NOT consume
 - opponent has no bounds on resources
 - consumption by opponent does not matter

What we want

- opponent's actions constrained
- consumption/production tracked
- a significant present-day issue ⇒ procurement of resources
 - limited amount on the market (or in nature)
 - acquisition cost depending on current availability

How we get it

Key notion ⇒ global availability of resources on the market

- a semantic component (part of the arena)
- evolves depending on agents' actions (also opponent)
- affects the choice of the actions (also opponent)

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Auxiliary notion ⇒ price of resources

- agents equipped with money instead of resources
- money for getting resources
- price of resources function of several components (take into account the history of the system)

Money

- inside the formula
- assigned to agents
- private: any agent has his own amount of money
- unknown
- availability checked for proponent's agents only

- part of the model
- represent the market (nature)
- public: agents draw on resources from a shared poo
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Money is a *meta-resource*

- represents several resource combinations
 - money like resources in previous approaches
- unit of measurement



Resource production and decidability

Alechina, Logan, Nga, Rakib

Actions can **only consume** resources

Bulling, Farwer

If actions may produce resources, then Model Checking becomes **UNDECIDABLE**

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Actions may produce resources...

- ...but not so much!!!
 - model checking decidable
 - several models fit (memory usage, leasing a car, releasing resources previously acquired)



Syntax and semantics

Formulae of PRB-ATL are given by the grammar:

$$\varphi ::= p \mid \neg \varphi \mid \varphi \land \varphi \mid \langle \langle A^{\$} \rangle \rangle \bigcirc \varphi \mid \langle \langle A^{\$} \rangle \rangle \varphi \mathcal{U} \varphi \mid \langle \langle A^{\$} \rangle \rangle \Box \varphi$$

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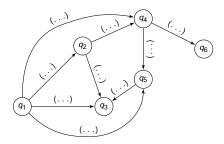
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Priced game structure

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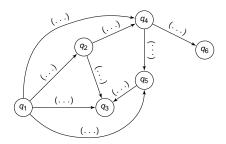


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- actions consume and produce resources
- resources have a variable prices
- transition guards: also opponent



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Model checking complexity

Theorem

The model checking problem for PRB-ATL is

- in EXPTIME (upper bound)
- PSPACE-hard (lower bound)

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ATL	RB-ATL	PRB-ATL
O(arphi imes G)	$O(\varphi ^{2\cdot r+1} \times G)$	$O(\varphi \times M^r \times S^n \times G)$

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Reduction from the *TQBF* problem

Fully Quantified Boolean Formula: all Boolean variables occur inside quantifier's scope



Reduction - the idea

- Given a fully quantified Boolean formula Φ (in prenex conjunctive normal form)
- We provide
 - a priced game structure G
 - a location q in G
 - an initial availability of resources \vec{m}
 - a PRB-ATL formula φ

such that

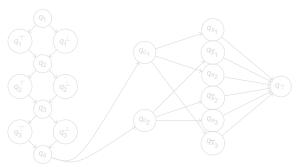
$$G, q, \vec{m} \models \varphi \text{ iff } \Phi \text{ is true}$$



Fully quantified Boolean formula:

$$\Phi = \exists x_1 \forall x_2 \exists x_3 [(x_1 \lor x_2 \lor \neg x_3) \land (\neg x_1 \lor \neg x_2 \lor x_3)]$$

- Initial availability of resources (6 resources 2 for each Boolean variable): $\vec{m} = \langle 1, 1, 1, 1, 1, 1 \rangle$ (only 1 item available for each resource)
- Priced game structure G_{Φ} corresponding to Φ (numer of agents: 1)



PRB-ATL formula $φ_Φ$ corresponding to Φ:

$$\langle\langle 1^{\vec{0}}\rangle\rangle \bigcirc \langle\langle 1^{\vec{0}}\rangle\rangle \bigcirc \langle\langle \emptyset^{\vec{0}}\rangle\rangle \bigcirc \langle\langle 1^{\vec{0}}\rangle\rangle \bigcirc \rho,$$

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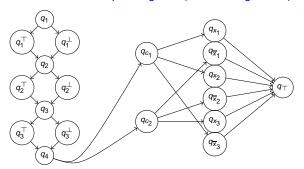
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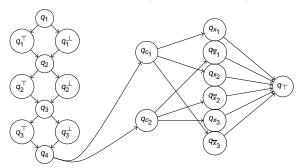
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Φ PRB-ATL formula $φ_Φ$ corresponding to Φ:

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Parametric PRB-ATL formulae

• PRB-ATL:

$$\varphi = \langle \langle A_1^{\$_1} \rangle \rangle \diamondsuit (\langle \langle A_2^{\$_2} \rangle \rangle \bigcirc p \lor \langle \langle A_3^{\$_3} \rangle \rangle q \mathcal{U} p)$$

Definition (Cost of a PRB-ATL formula)

$$f_{-}cost(\varphi) = \$_{1}(A_{1}) + \$_{2}(A_{2}) + \$_{3}(A_{3})$$

 $\bullet \ \, \text{parametric PRB-ATL:} \quad \, \varphi_{\vec{X}} = \langle \langle X_1^{\$_1} \rangle \rangle \diamondsuit \big(\langle \langle X_2^{\$_2} \rangle \rangle \bigcirc p \vee \langle \langle A_3^{\$_3} \rangle \big\rangle q \mathcal{U} p \big)$

The Optimal Coalition problem

Definition (Optimal Coalition problem)

To determine minimal-cost coalitions that satisfy a PRB-ATL formula

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- a location
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Theorem

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- in EXPTIME
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Conclusions

A logic for modeling multi-agent systems with bounds on resources

ATL: abilities of coalitions of agents

RB-ATL: abilities of coalitions whose agents are equipped with a finite endowment of resources

PRB-ATL: abilities of coalitions whose agents are equipped with an amount of money

- global availability of resources
- money price of resources

Future work

Resource-bounded extensions of other classical formalisms

▶ e.g., μ-calculus [Della Monica, Lenzi - ICAART 2012]

Hierarchical, MAS, and resources???

Future work

- Resource-bounded extensions of other classical formalisms
 - e.g., μ-calculus

[Della Monica, Lenzi - ICAART 2012]

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Future work

- Resource-bounded extensions of other classical formalisms
 - e.g., μ-calculus

[Della Monica, Lenzi - ICAART 2012]

• Hierarchical, MAS, and resources???