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$$= \sum_{i=k-h}^{\infty} \, \left(\begin{matrix} n-h+(k-1)(2-i) \\ i \end{matrix} \right)$$

= v_n , as required.

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A NEW IMPORTANT FORMULA FOR LUCAS NUMBERS

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The formula

(1)
$$\frac{L_{10n}}{L_{2n}} = (L_{4n} - 3)^2 + (5F_{2n})^2$$

may be easily verified putting $L_n = \alpha^n + \beta^n$,

$$F_n = \frac{\alpha^n - \beta^n}{\sqrt{5}}$$
, $\alpha\beta = -1$,

Since for n>0, (1) gives a decomposition of $\,L_{10n}\,/L_{2n}\,$ into a sum of 2 squares, and since any divisor of a sum of 2 squares is -1 (mod 4), it follows that any primitive divisor of $\,L_{10n},\,\,n>0,\,\,$ is -1 (mod 4).
