The Fibonacci Quarterly 1993 (vol.31,3): 194-204

ADDENDUM TO
"Second Derivative Sequences of Fibonacci and Lucas Polynomials"

by

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In the above paper [1], the proof of Proposition 9 was inadvertently omitted. It reads as follows:

Proof of Proposition 9: From (1.8) we have

$$\begin{aligned} C_n &= \sum_{i=0}^{n} F_i^{(1)} F_{n-i} = \frac{1}{5}\left(\sum_{i=0}^{n} iL_i F_{n-i} - \sum_{i=0}^{n} F_i F_{n-i}\right) \\ &= \frac{1}{5}\sum_{i=0}^{n} iF_n + \frac{1}{5}\sum_{i=0}^{n} i(-1)^i F_{n-2i} - \frac{1}{5}\sum_{i=0}^{n} F_i F_{n-i}. \end{aligned} \tag{5.11}$$

From (5.1) and (5.3), (5.11) can be rewritten as

$$\begin{aligned} C_n &= \frac{1}{10}[n(n+1)F_n] - \frac{1}{25}(nL_{n+1} + 2F_n) - \frac{1}{25}(nL_n - F_n) \\ &= \frac{1}{50}[5n(n+1)F_n - 2F_n - 2nL_{n+2}] = \frac{1}{50}[(5n^2-2)F_n + 5nF_n - 2nL_{n+2}] \\ &= \frac{1}{50}[(5n^2-2)F_n - n(2L_{n+2} - 5F_n)] = \frac{1}{50}[5n^2-2)F_n - 3nL_n] = F_n^{(2)}/2. \quad \square \end{aligned}$$

Additional comment: With regard to Conjectures 1-7 in [1], some of which were known by us to be true, we wish to record that, in private correspondence with us, both Richard André-Jeannin and David Zeitlin have independently established the validity of these Conjectures.

REFERENCE

1. P. Filipponi & A. F. Horadam. "Second Derivative Sequences of Fibonacci and Lucas Polynomials." *The Fibonacci Quarterly* **31.3** (1993):194-204.

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