



# Video analysis in Pan-Tilt-Zoom camera networks

Dr. Christian Micheloni  
Dept. Computer Science  
University of Udine





- Material
  - <http://users.dimi.uniud.it/~christian.micheloni/PTZ4ICDSC.html>
- Acknowledgements
  - Dr. Claudio Piciarelli, University of Udine for the cooperation on PTZ network reconfiguration.
  - Dr. Sanjeev Kumar, University of Roorke for the work on Stero-PTZ object localization
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- Video Sensor Networks provide security by deploying video cameras.
- Greater security requires more cameras
  - Wide Vs. Narrow angle of view (resolution Vs. coverage)
  - Non overlapping FOVs limit processing accuracy
    - Occlusions
    - Localization
  - Overlapping FOVs requires huge amount of cameras

C. Micheloni, B. Rinner, G.L. Foresti, «Video Analysis in Pan-Tilt-Zoom Camera networks», *IEEE Signal Processing Magazine*, vol.27, no.5, pp.78-90, Sept. 2010.



- Pan-Tilt-Zoom cameras by adapting the FOV can limit such a requirement.
  - High resolution
  - Overlap FOV to solve occlusion, localization and tracking
- PTZs on the other hand introduce new problems:
  - Ego-Motion estimation
    - Low level motion detection techniques cannot be directly exploited
  - Calibration requires new solutions

C. Micheloni, B. Rinner, G.L. Foresti, «Video Analysis in Pan-Tilt-Zoom Camera networks», *IEEE Signal Processing Magazine*, vol.27, no.5, pp.78-90, Sept. 2010.

- Aloimonos proposed the active vision paradigm to describe the dynamic interaction between the observer and the object observed to actively decide what to see.

**With PTZ cameras we want to decide**

**Where**

**What**

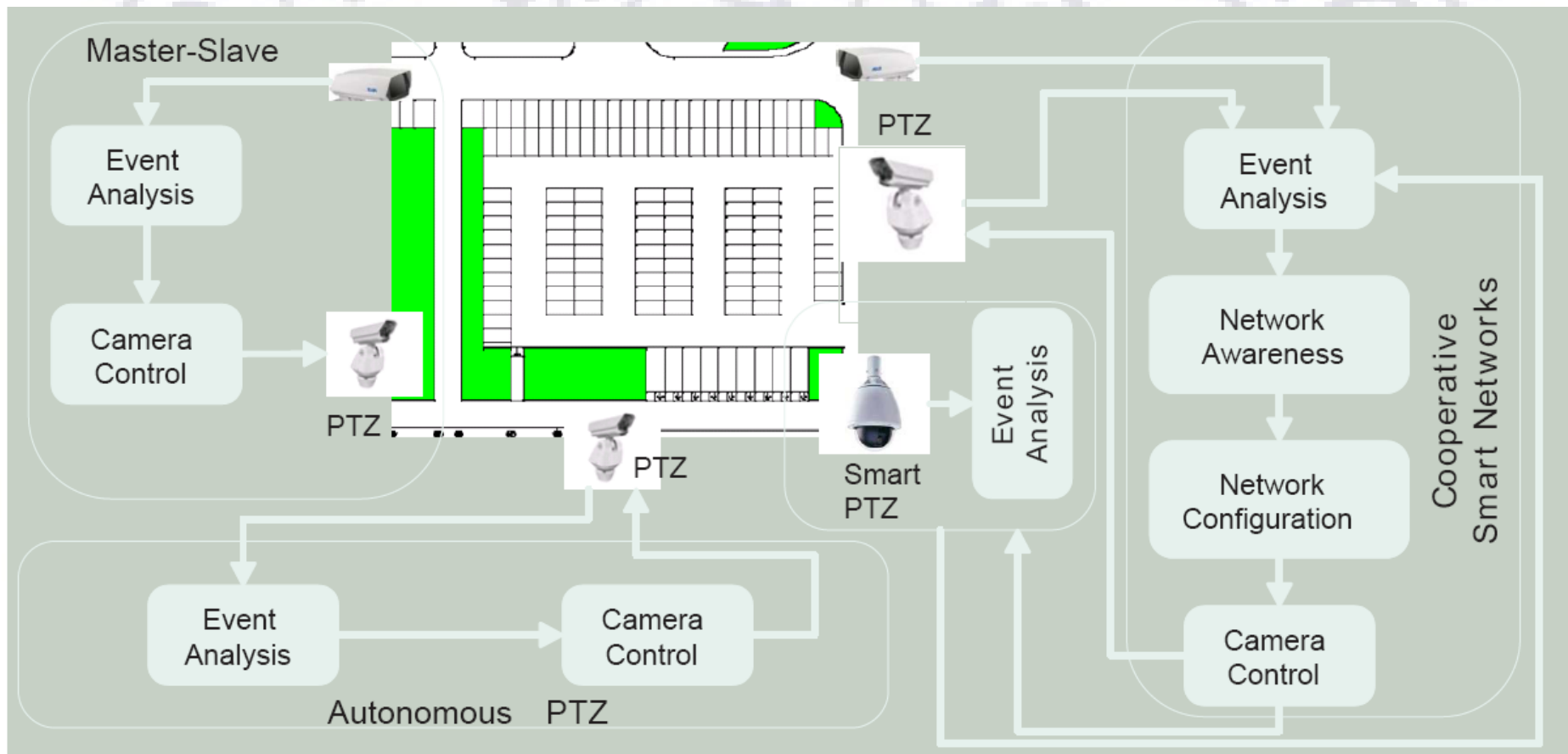
**How**

**looking at the scene**

Y. Aloimonos. Active Perception. Lawrence Erlbaum Associates, 1993.

# Evolution of PTZ usage

- From master slave to cooperative smart networks



C. Micheloni, B. Rinner, G.L. Foresti, «Video Analysis in Pan-Tilt-Zoom Camera networks», *IEEE Signal Processing Magazine*, vol.27, no.5, pp.78-90, Sept. 2010.

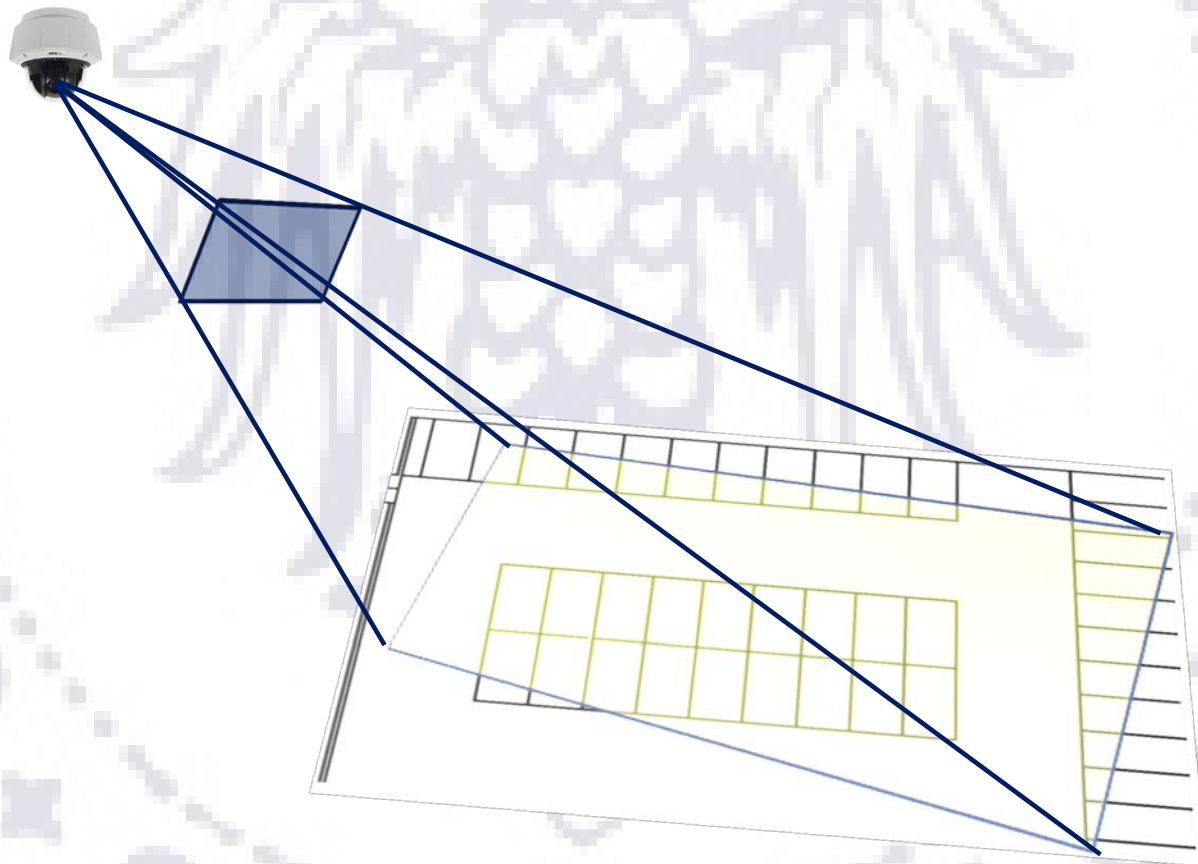


# Where is a PTZ looking at?

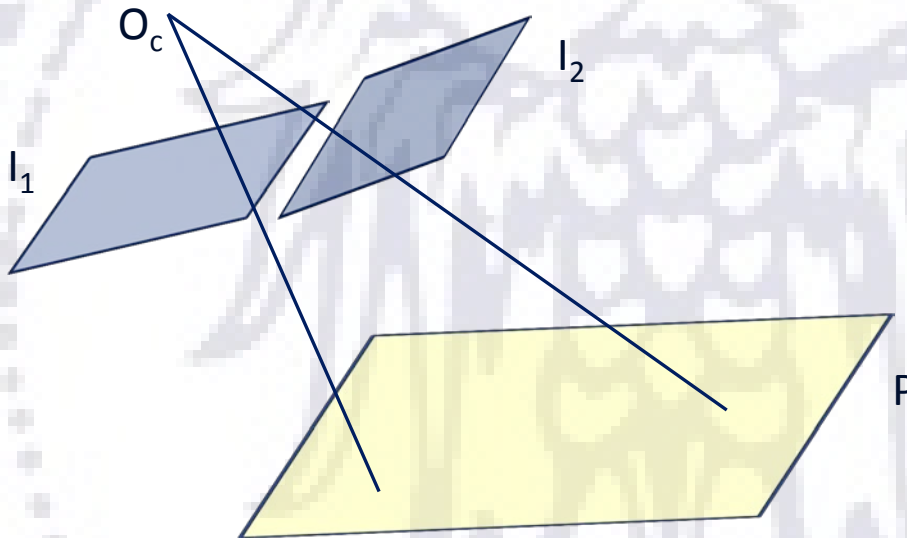
The estimation of the PTZ field of view  
while moving



- The area covered is the projection of the Image plane to the ground. Usually a convex polygon.



- If space points are coplanar then there is a projective transformation  $H$  between the world  $P$  and image plane  $l^1$ .



$$p_{i_1} = H_1 P$$

$$p_{i_2} = H_2 P$$

$$H_{3 \times 3} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{bmatrix}$$

- Easy to compute: at least 4 points of  $P$  matching in  $l$ .

## Problem

**We need a homography for each combination of P,T,Z parameters**

<sup>1</sup>R. Hartley and A. Zisserman, Multiple View Geometry in Computer Vision, Cambridge University Press



- Full calibration of the PTZ camera
  - S. N. Sinha and M. Pollefeys, "Pan-tilt-zoom camera calibration and high-resolution mosaic generation", Computer Vision and Image Understanding, Vol. 103, Issue 3, Sep. 2006, pp. 170–183
- Homography estimation
  - I. N. Junejo and H. Foroosh Optimizing PTZ camera calibration from two images, Machine and Vision Applications, Vol. 23, No 2 (2012), pp.375-389
- Trigonometry

# Homography Estimation

$I_1(\varphi_c^1, \theta_c^1, Z_c^1)$



$I_2(\varphi_c^2, \theta_c^2, Z_c^2)$



M

$$M = H_{I_1, M} I_1$$

$$M = H_{I_2, M} I_2$$

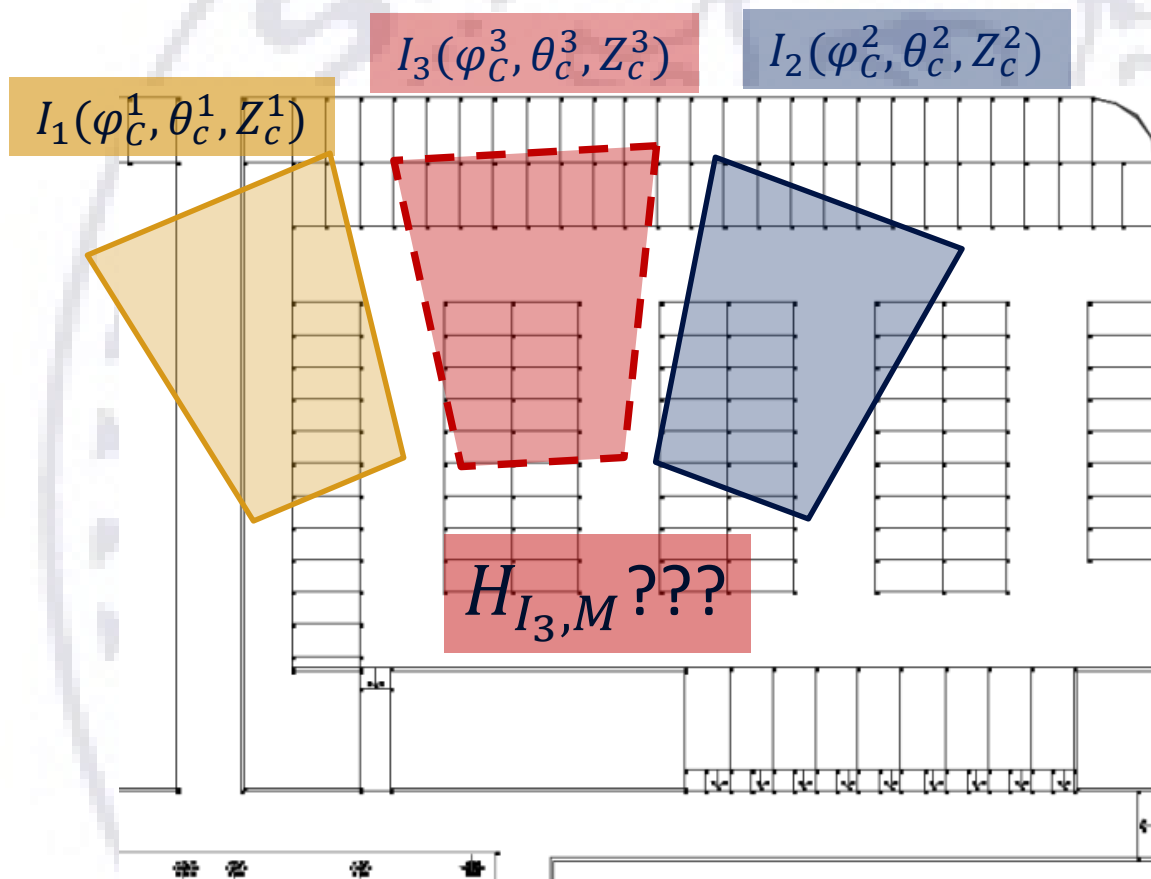
$$H_{I_2, M}^{-1} M = I_2$$

$$H_{I_2, M}^{-1} M = H_{I_2, M}^{-1} H_{I_1, M} I_1 = I_2$$

$$H_{I_1, I_2} = H_{I_2, M}^{-1} H_{I_1, M}$$

**Problem: I need to compute  $H_{I_1, I_2}$  for all  $I_2$  given  $H_{I_1, M}$**

# Homography Estimation



We have

$$H_{I_2,M}$$

$$H_{I_1,M}$$

- Compute sift matching between  $I_3$  and  $I_1/I_2$
- Compute  $H_{I_3,I_1}$  and  $H_{I_3,I_2}$
- Select the one that minimizes the errors

$$H_{I_3,M} = H_{I_1,M} * H_{I_3,I_1} * I_3$$

$$H_{I_3,M} = H_{I_2,M} * H_{I_3,I_2} * I_3$$

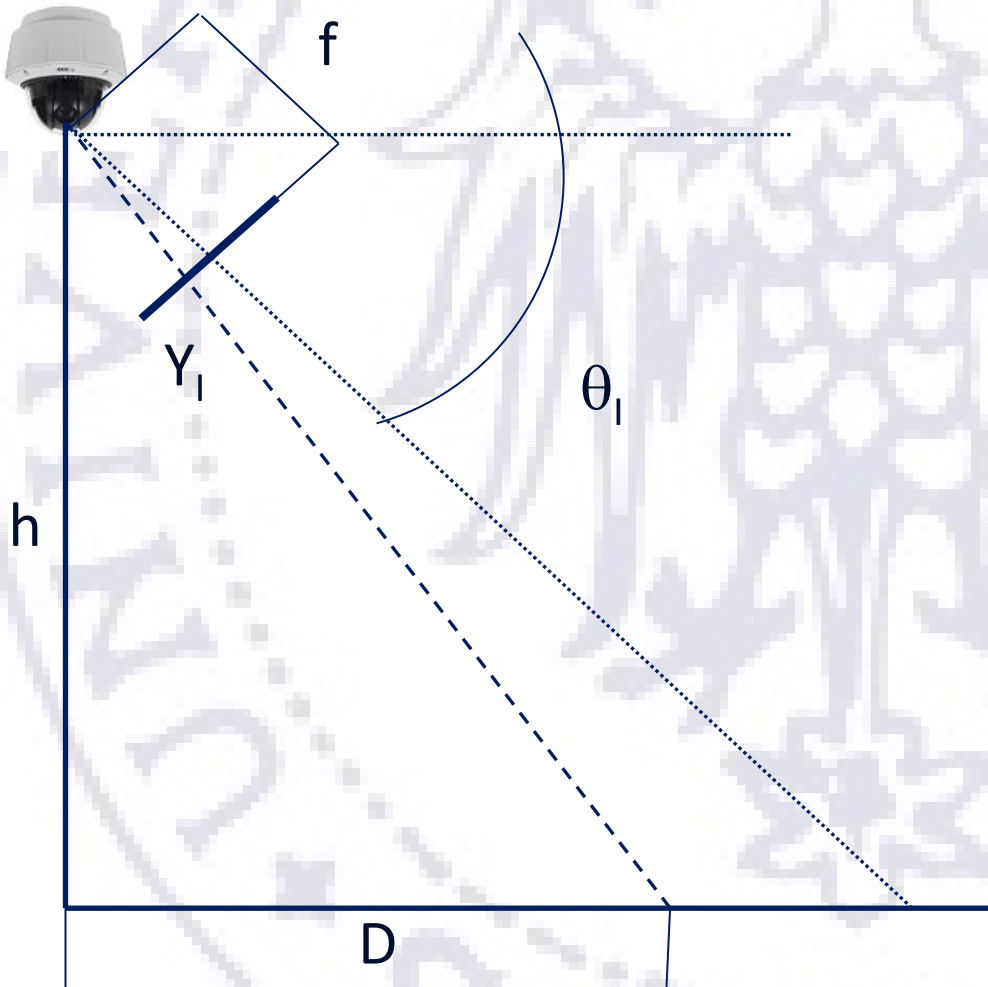
**Problem: sift/surf are not fast**



- Useful when the environment is not well structured then does not allow full vision approaches.
- It is required:
  - To be able to read camera parameters
  - To know the position of the camera reference system with respect to the world reference system
  - The camera should incorporate an algorithm to center a camera point into the center of the image by panning and tilting.

# From camera to world

- An image point  $(x_I, y_I)$  can be projected into the world by using geometric properties



$$\theta_I = \text{func}(f, y_I, \theta_c)$$

$$D = h * \text{ctan}(\theta_I)$$

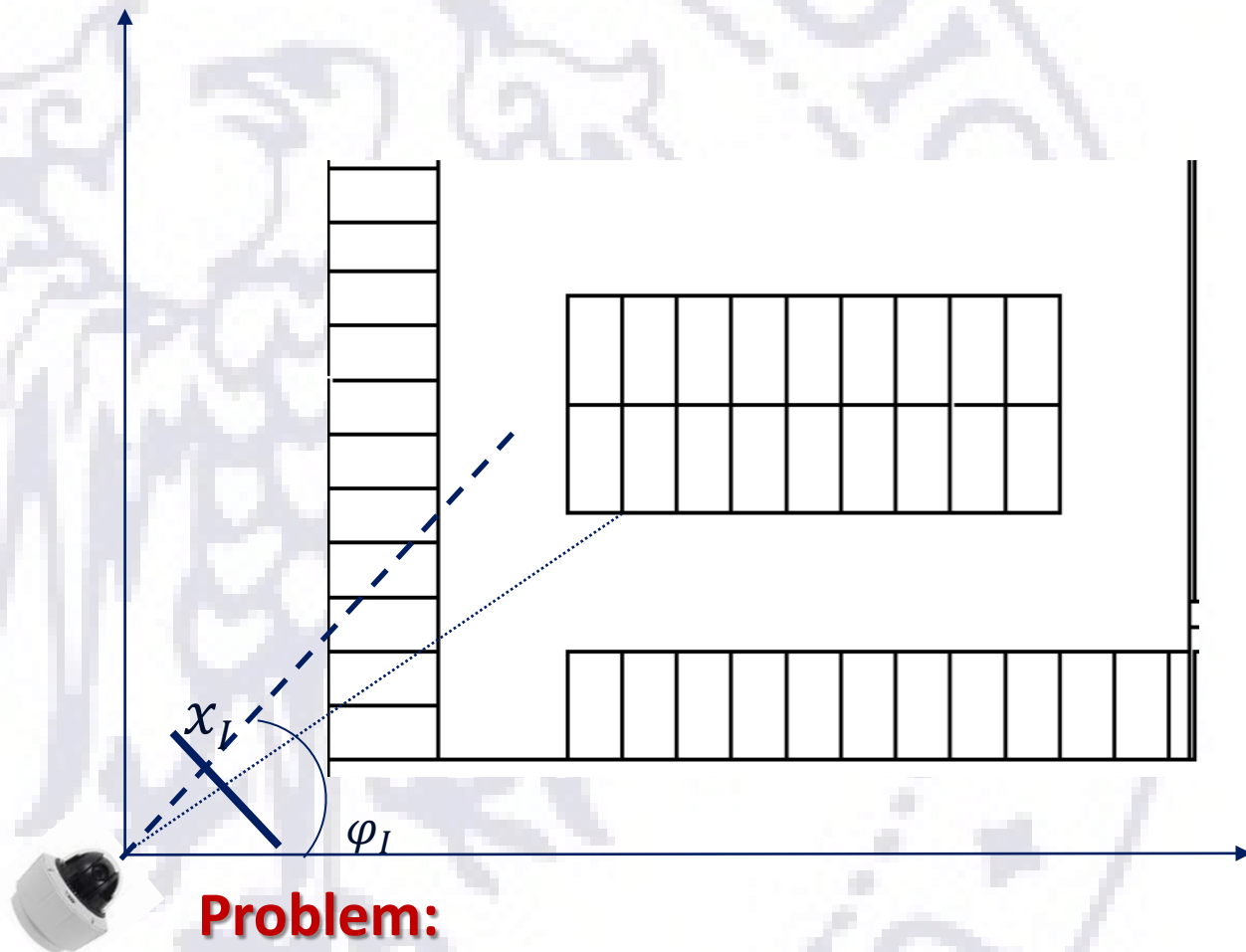
$\varphi_C$  Pan angle of the camera

$\theta_C$  Tilt angle of the camera

$$X_m = D * \cos(\varphi_I)$$

$$Y_m = D * \sin(\varphi_I)$$

$$\varphi_I = \text{func}(f, x_I, \varphi_c)$$

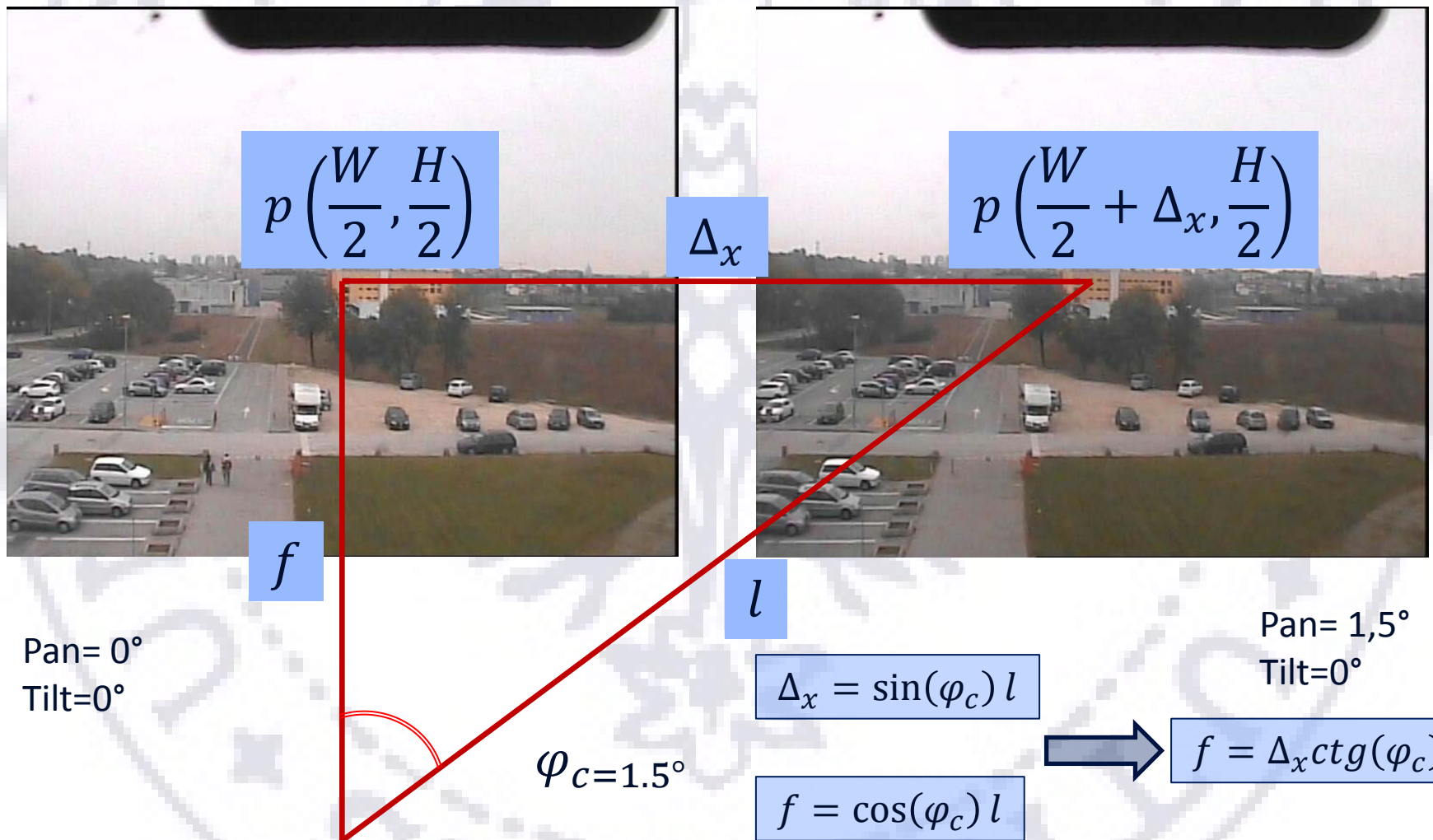


**Problem:**

**We do not read the focal length from the camera. We read the zoom step  $Z$**

**We can estimate  $f = \text{func}(Z)$**

- Center the camera on two different points lying on the central line



Zoom 1



Zoom 100

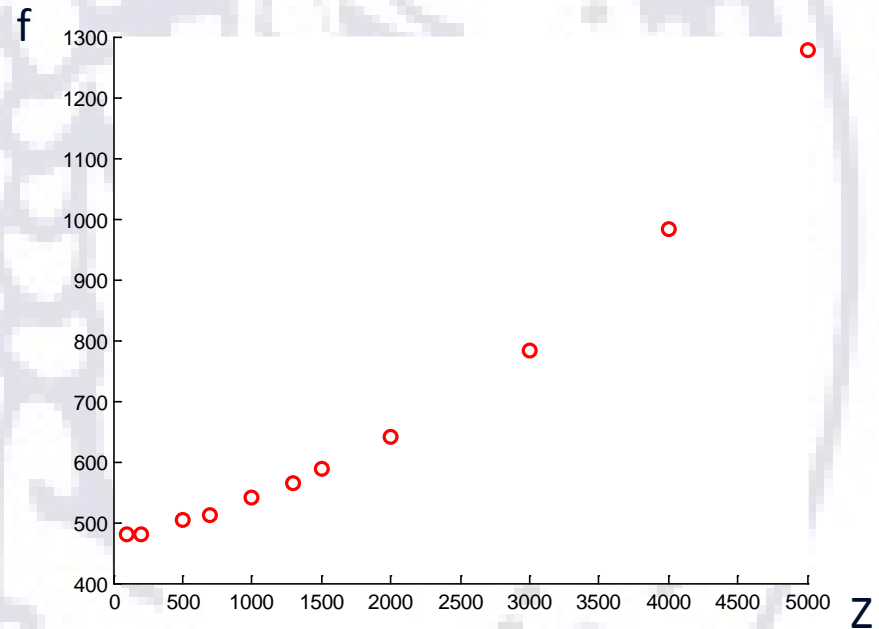


⋮

Zoom 600



⋮



Zoom 1



Zoom 100

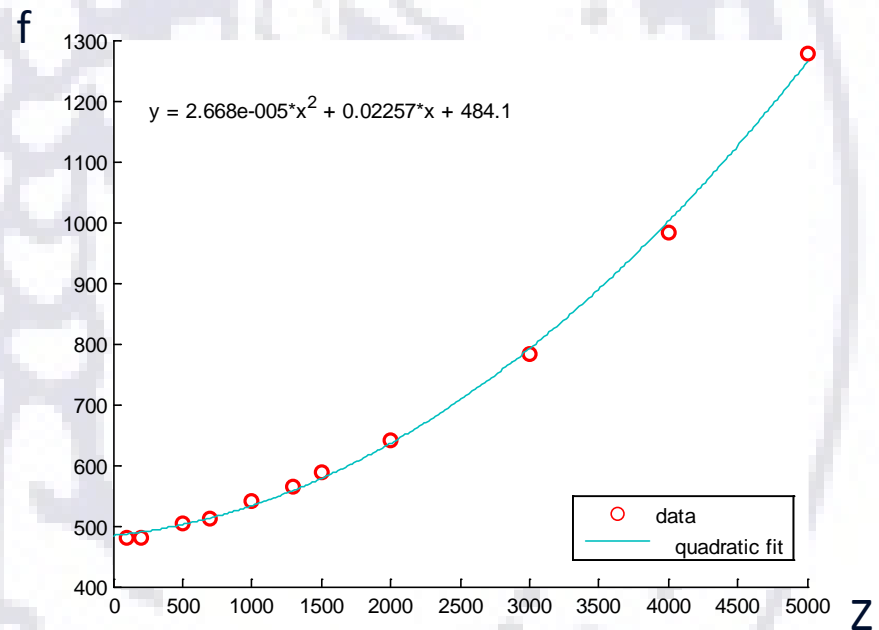


...

Zoom 600



...



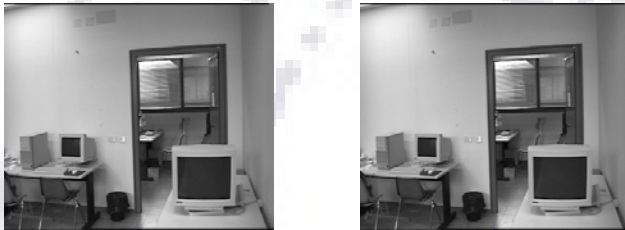


# What is a PTZ looking?

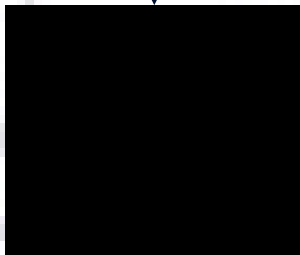
Detecting and tracking moving objects



Static camera



Change detection



PTZ camera



Change detection



Compensation of the motion induced  
by the camera

- 9 Areas of tracking
- Area Alignment
- Best 3 used for Affine Computation



- Computation of clusters

$$C_w(d) = \{f_i \in TFS_w \mid d_i = d\}$$

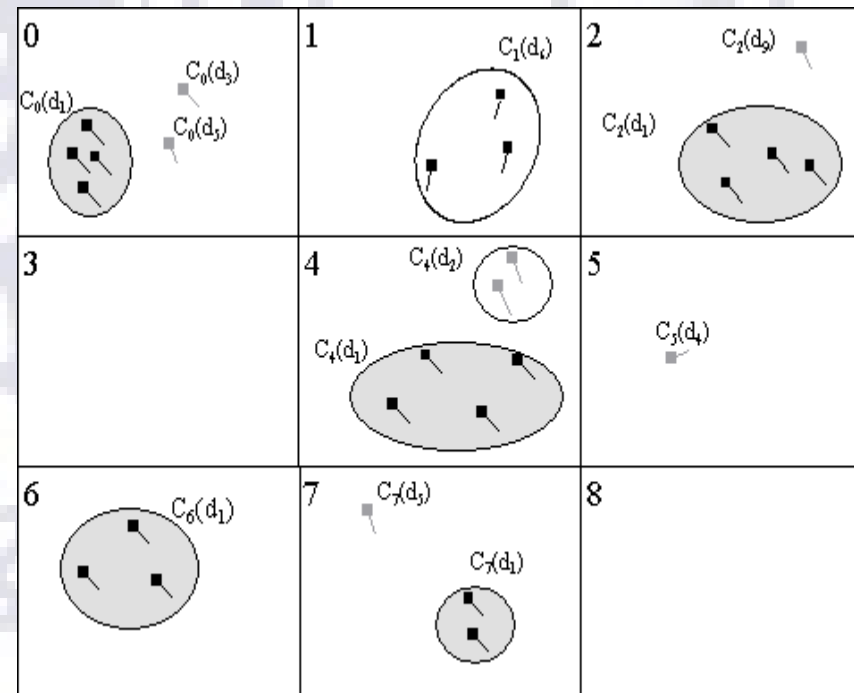
- Selection of the best cluster for each area

$$RF(C_w(d_k)) = \frac{\sum_{f_j \in C_w(d_k)} E_{f_j}}{|C_w(d_k)|^2}$$

- Selection of the best feature for each of the 3 best clusters

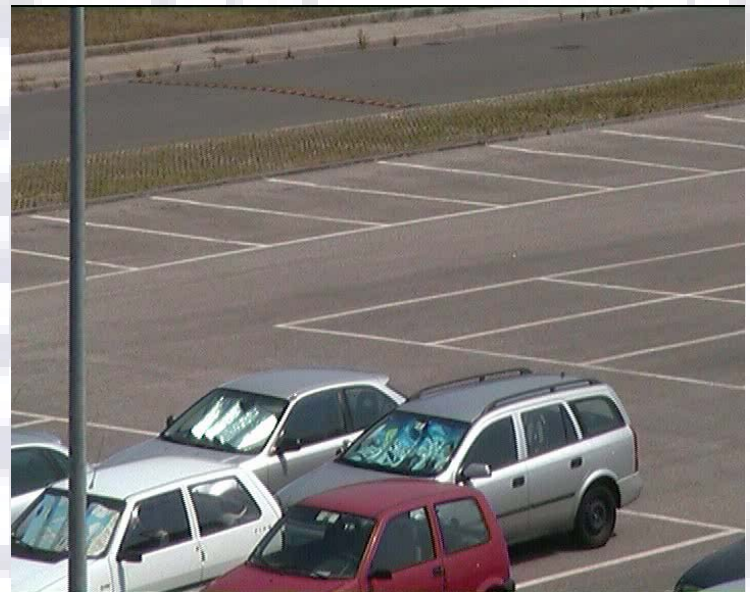
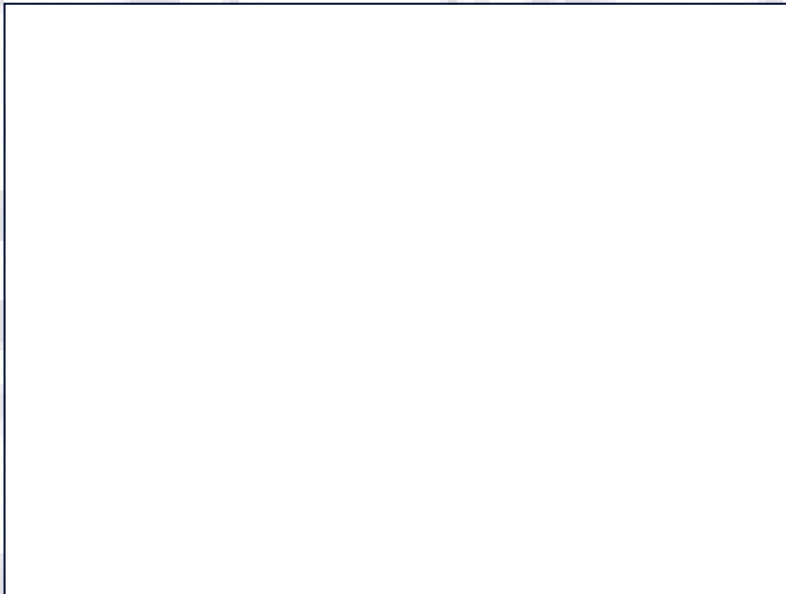
$E_{f_i}$  is the residual or the error in tracking the feature  $i$

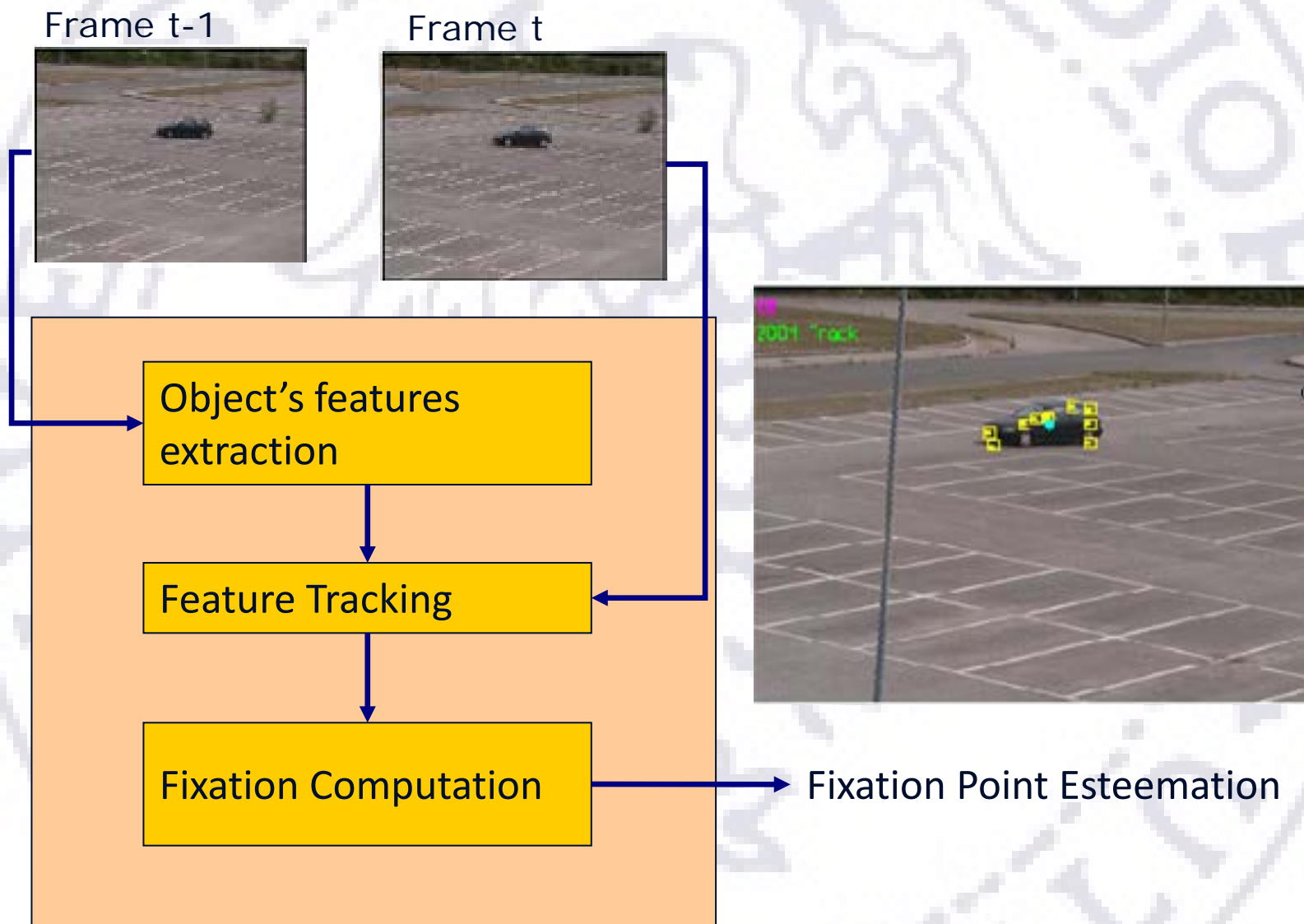
$$f'_i = \underbrace{\begin{pmatrix} a_1 & a_2 & a_5 \\ a_3 & a_4 & a_6 \\ 0 & 0 & 1 \end{pmatrix}}_A f_i$$



Registration is performed on the basis of an affine transform







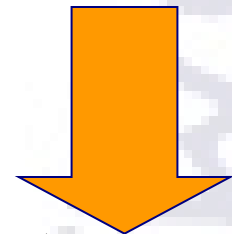
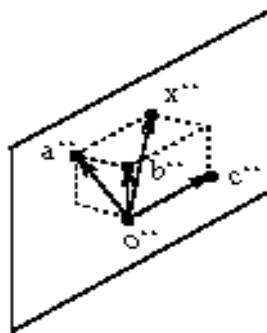
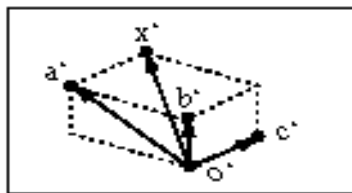
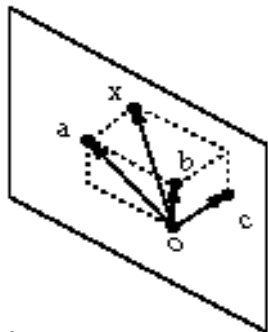
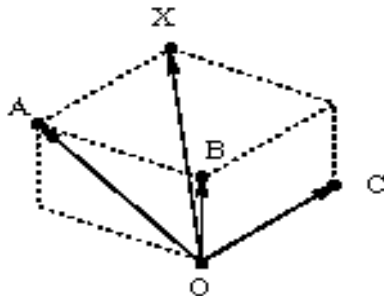
Affine transfer



Planar Points

$$g' = Ng + r$$

$$N = \begin{pmatrix} n_1 & n_2 \\ n_3 & n_4 \end{pmatrix} \quad r = \begin{pmatrix} r_1 \\ r_2 \end{pmatrix}$$

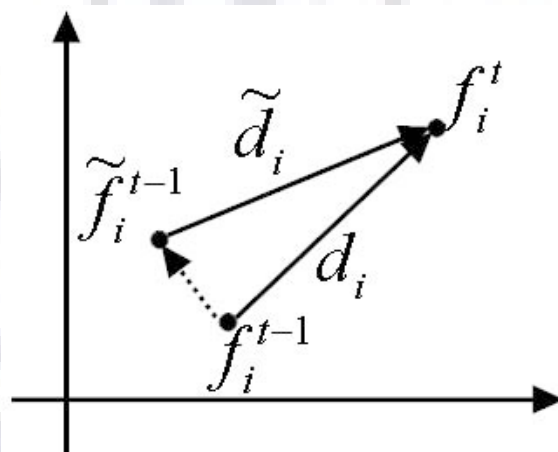


$$\begin{pmatrix} x_1' & y_1' & 1 \\ x_2' & y_2' & 1 \\ \vdots & \vdots & \vdots \\ x_n' & y_n' & 1 \end{pmatrix} \begin{pmatrix} n_1 \\ n_2 \\ r_1 \end{pmatrix} = \begin{pmatrix} x_1' \\ x_2' \\ \vdots \\ x_n' \end{pmatrix}$$

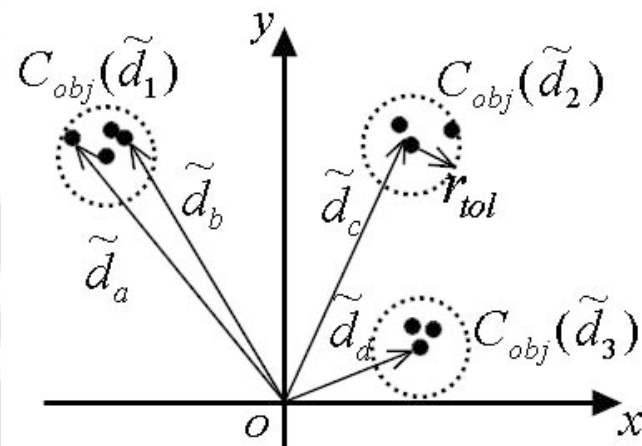
Tordoff- Murray – PAMI, January 2004

- Least square
- SVD





$$\tilde{d}_i = f_i^t - \tilde{f}_i^{t-1} = f_i^t - \tilde{A}f_i^{t-1}$$




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## Algorithm 1 Clustering

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**repeat**

Feature extraction and tracking

Clusters computation

Background cluster deletion

Computation of the centre of mass for each cluster

**until** zooming

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## Localization in PTZs network

From static-PTZ to PTZ-pair cooperation  
exploiting stereo vision



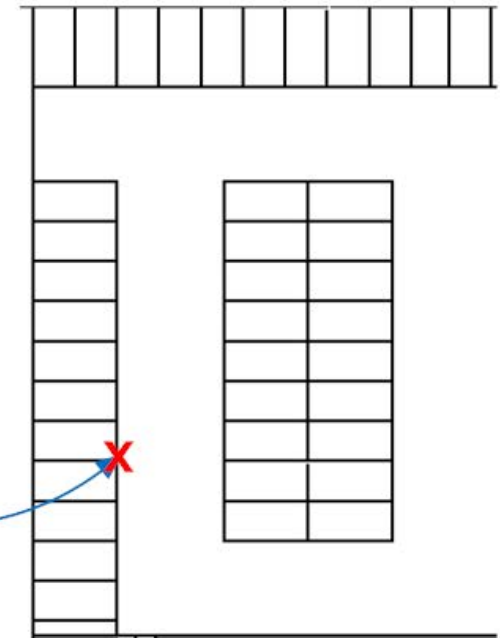
## What is localization?

The task of localization is to localize a object/target (moving, static) on a given test-map.

Generally, localization is made by taking the intersection of optical axis with the ground position of object/target in respective frames.



Image frame

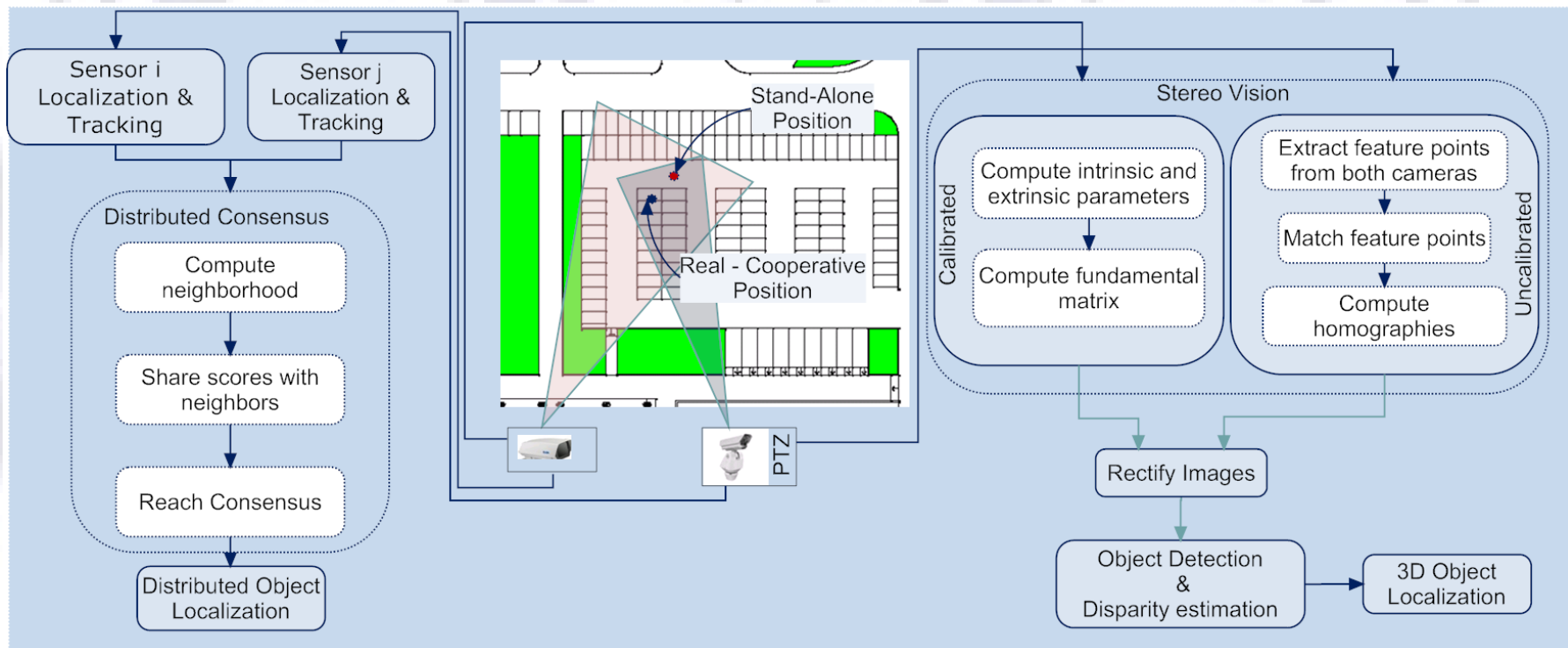


Ground plane Test-map

**What happens in the case of partially occluded object? Means, where ground position of object/target is occluded by some other objects.**



Erroneous localization using monocular camera based techniques.



Technique	Advantage	Disadvantage
Centralised	Complete network information Pixel level fusion	High bandwidth usage Affected by occlusions
Distributed	Dynamic network topology  Distributed consensus Low bandwidth usage Ad-hoc network communication	Accuracy depending on single camera estimations Affected by occlusions
Stereo	Precise 3D localisation Occlusions free	Constrained points of view Base line constrained

R. Olfati-Saber, J. Fax and R. Murray. Consensus and cooperation in networked multi-agent systems. Proceedings of the IEEE, 95(1):215-233, 2007

C. Soto, B. Song and A. Roy-Chowdury. Distributed multi-target tracking in a self-configuring camera network. In IEEE Conference on Computer Vision and Pattern Recognition, pp 1486-1493, 2009

Bi Song, D. Chong, A.T. Kamal, J.A. Farrell and A. Roy-Chowdury, Distributed Camera Networks, IEEE Signal Processing Magazine, Vol. 28, No. 3, pp. 20-31, 2011



- Stereo vision: To extract 3-D information of a real world scene/object from its two or more 2-D images [2, 5].
- Steps:
  1. Calibration,
  2. Rectification,
  3. Stereo Matching
- Remarks: Generally, a pair of cameras having equal internal image parameters and fixed field of views are used in classical stereo systems.



- Use of a pair static-PTZ cameras as a stereo system.

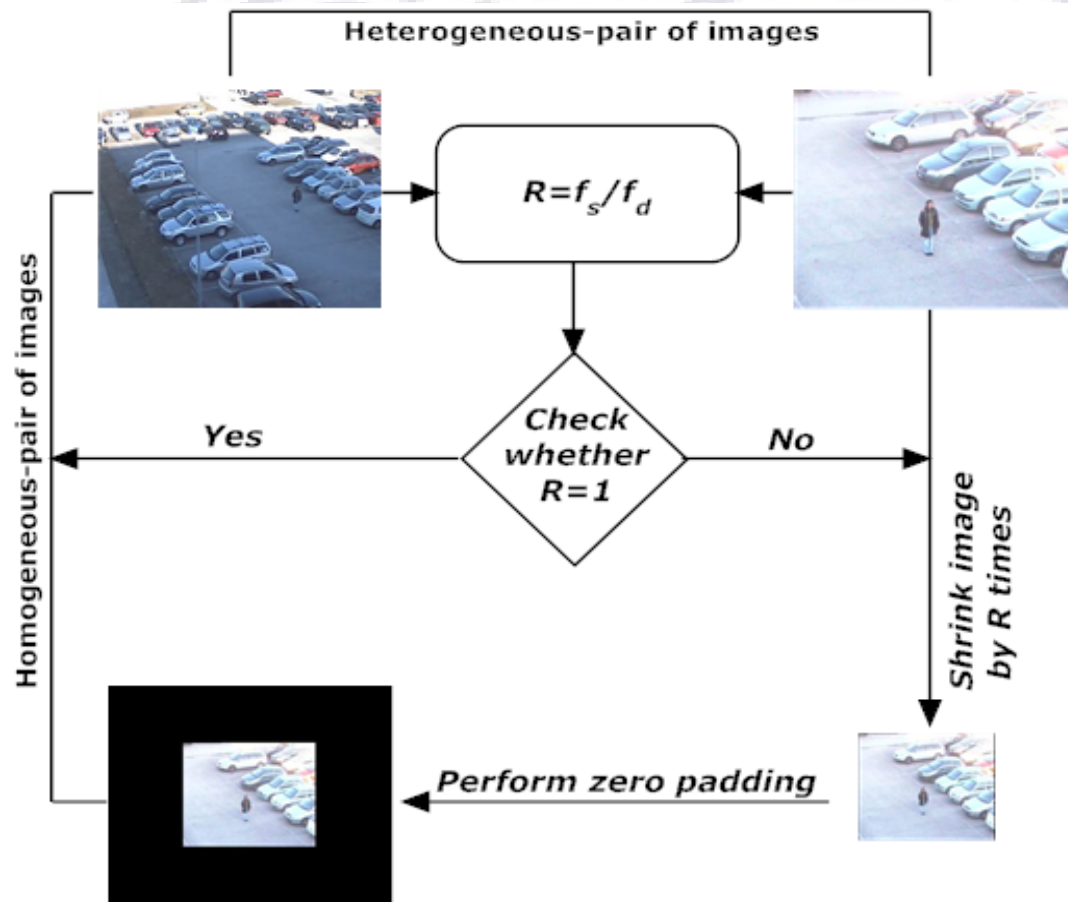
Abidi, B., Koschan, A., Kang, S., Mitckes, M., Abidi, M., 2003. Automatic Target Acquisition and Tracking with Cooperative Static and PTZ Video Cameras. Kluwer Academic, Ch. Multisensors Surveillance Systems: The Fusion, pp. 43–59.

Chen, C. H., Yao, Y., Page, D., Abidi, B., Koschan, A., Abidi, M., 2008. Heterogeneous fusion of Omni-directional and PTZ cameras for multiple object tracking. IEEE Transaction on Circuit and Systems for Video Technology 18(8), 1052–1063

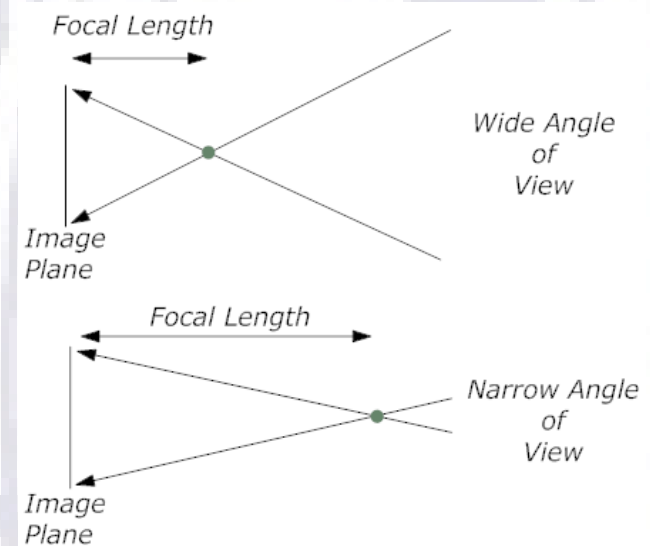
Kumar, S., Micheloni, C., Piciarelli, C., Foresti, G. L., 2009. Stereo localization based on network's uncalibrated camera pairs. In: Sixth IEEE International Conference on Advanced Video and Signal Based Surveillance. pp. 502–507.

- Advantage: More degree of freedoms in terms of
  - Angle of Views
  - Field of views
  - Zoom (close or wide focus according to the requirement)
- Difficulties:
  - To calibrate PTZ camera is very difficult for each position in real time applications.
  - Heterogeneity involved in internal camera parameters.

# Compensation of the heterogeneity

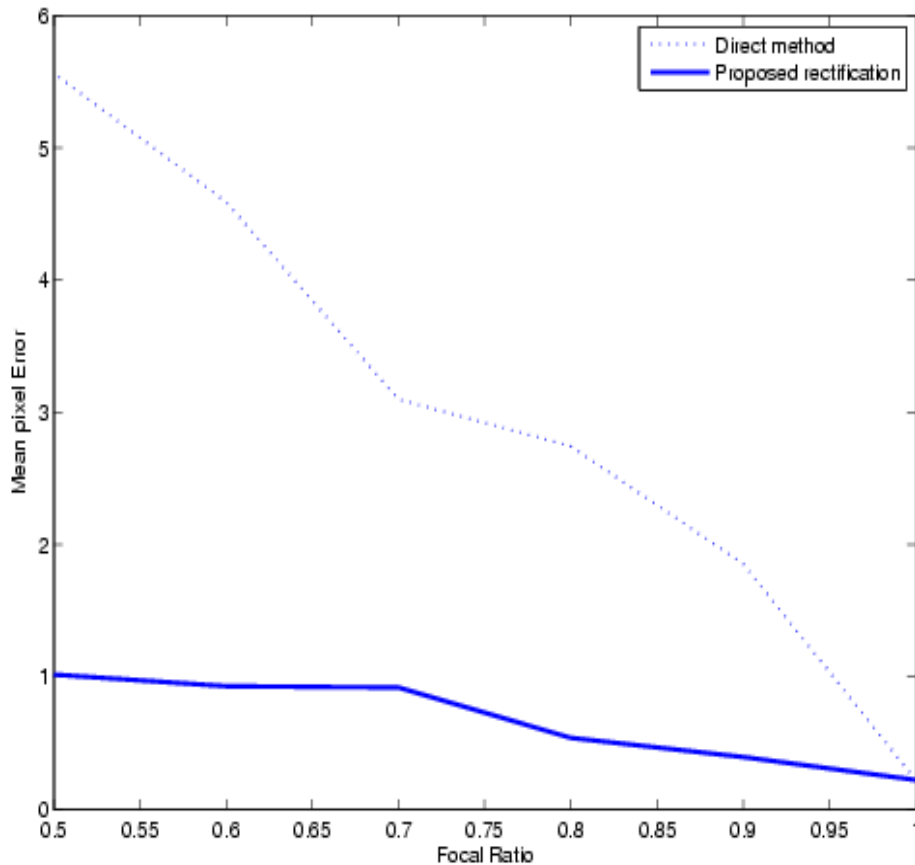


**Idea:** Focal length is inversely proportional to field of view.



# Rectification Results

**Mean-Error between epipolar lines in rectified pairs of images  
(Kumar et al Vs. Hart et al.)**



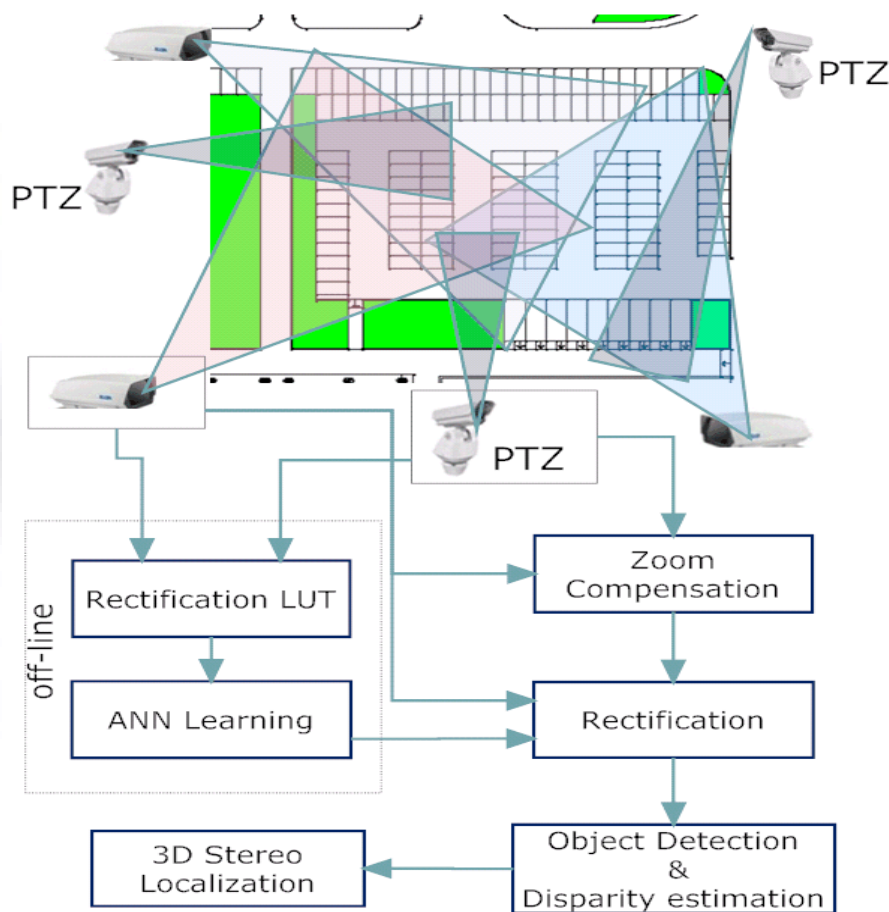
**Direct method<sup>2</sup>:** Rectification using image pairs without compensating the effect of heterogeneity in internal image parameters.

**Homogeneous rectification<sup>1</sup>:** Rectification made after making image pairs as homogeneous in terms of internal image parameters.

Kumar, S., Micheloni, C., Piciarelli, C., Foresti, G. L., 2009. Stereo localization based on network's uncalibrated camera pairs. In: Sixth IEEE International Conference on Advanced Video and Signal Based Surveillance. pp. 502–507.

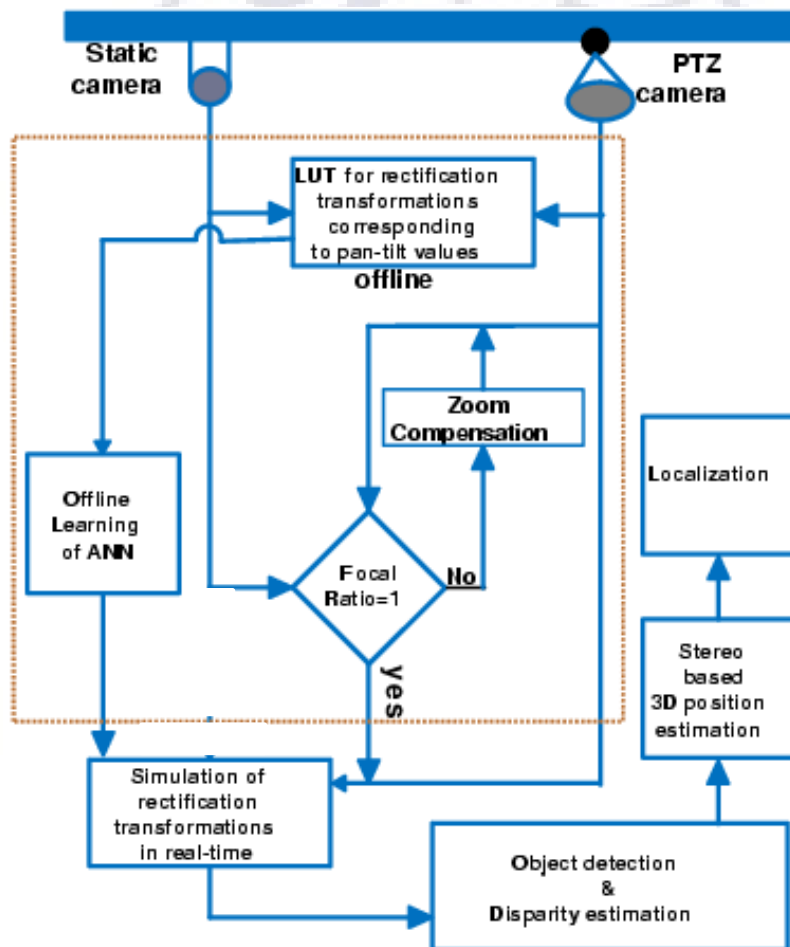
Hart, J., Scassellati, B., Zucker, S., 2008. Epipolar geometry for humanoid robotic heads. In: International Cognitive Vision Workshop. pp. 24–36.

## System architecture:



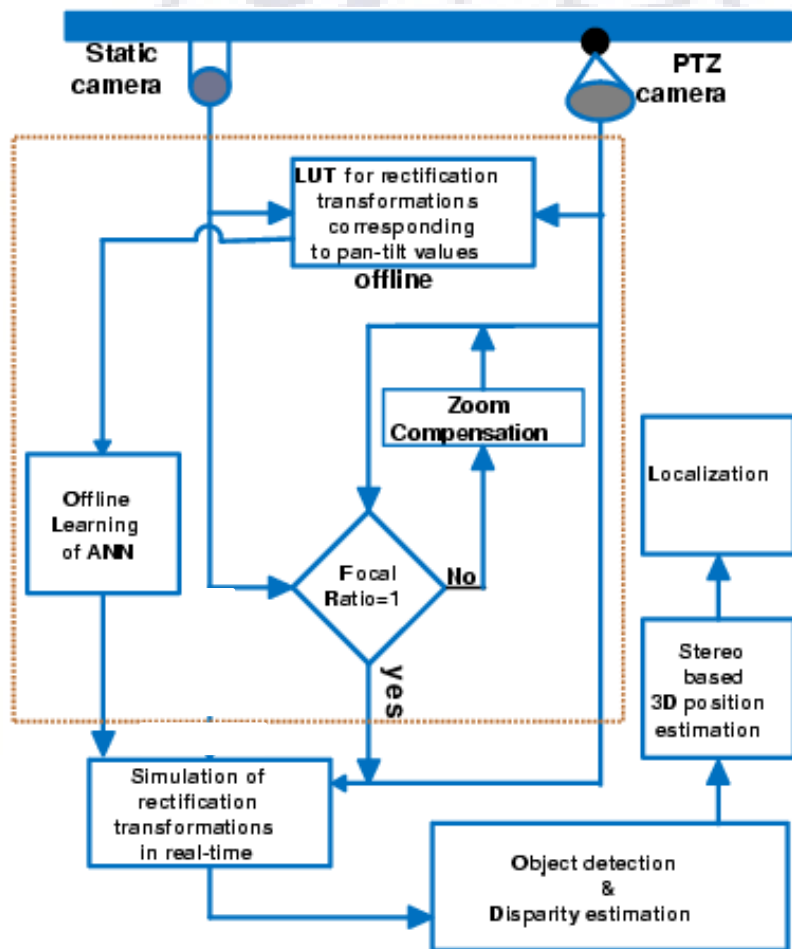
In a network containing various PTZ and static cameras, cooperativeness between various cameras involved for considering following two points

- Once the target is selected in any static camera then selection of nearest PTZ camera for stereo vision task.
- Once the target move away from the field of view of respective static camera then the selection of next static camera based on the trajectory created by PTZ camera based on the motion of target.



## Main steps: Offline

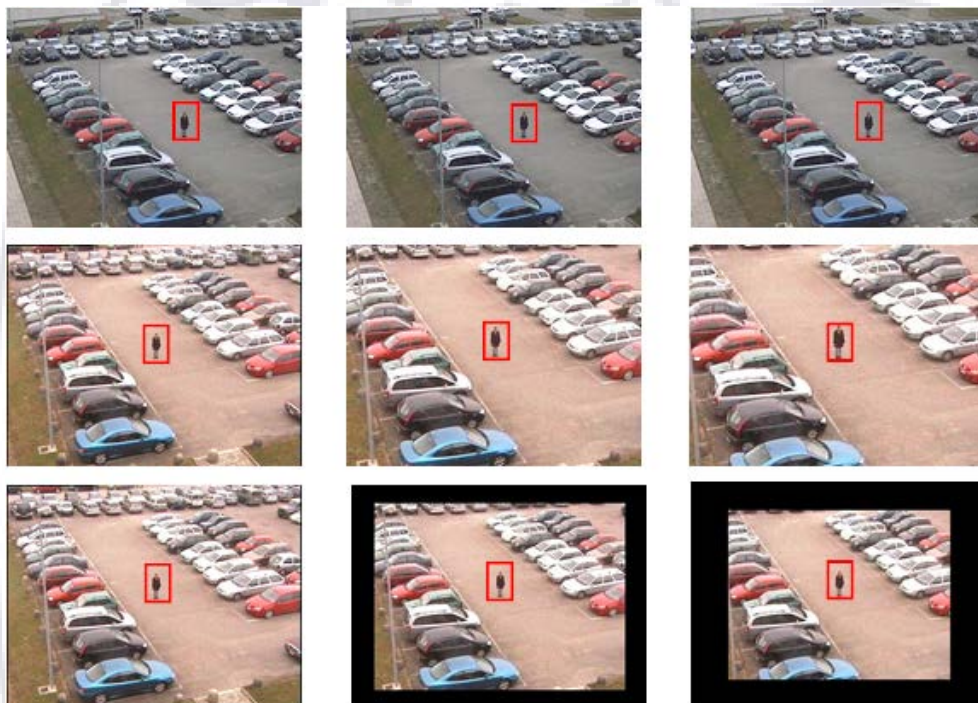
1. Sampling of pan-tilt angles for the PTZ camera.
2. Construction of LUT for rectification transformation for each possible pairs of static-PTZ cameras.
3. Train neural network



Main steps: Online

1. Select target with a static camera
2. Redirect the nearest PTZ camera
3. Grab image sequences from both cameras.
4. Acquire Pan and Tilt Information for a grabbed image
5. Interpolate rectification transformation using NN-based interpolation.
6. Rectify stereo sequences and compute disparity for target position
7. Computer stereo based 3D position of object
8. Make localization

## Results in unequal zoom case



Static camera frames

PTZ camera frames

PTZ camera frames (after zoom compensation)

## Localization

- + Proposed stereo localization
- \* Kinematics chain app. (Hart et al., 2008)
- x Monocular localization

\*J. Hart, B. Scassellati and S.W. Zucker. Epipolar Geometry for Humanoid Robot Localization, Proc. Of 4th International Cognitive Vision Workshop, 24–36, 2008.

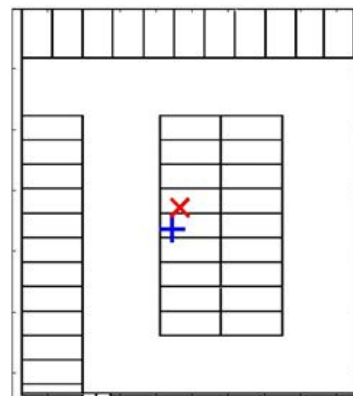
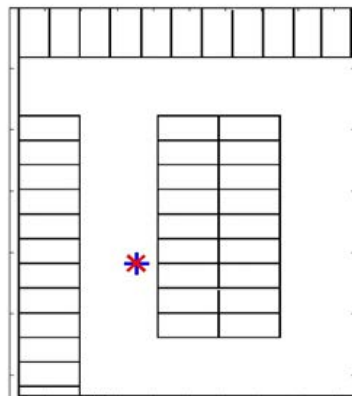
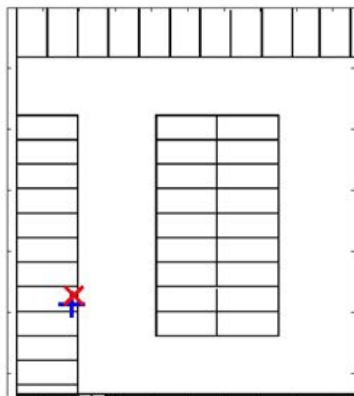
## Results in case of partially occluded target



Static camera frames



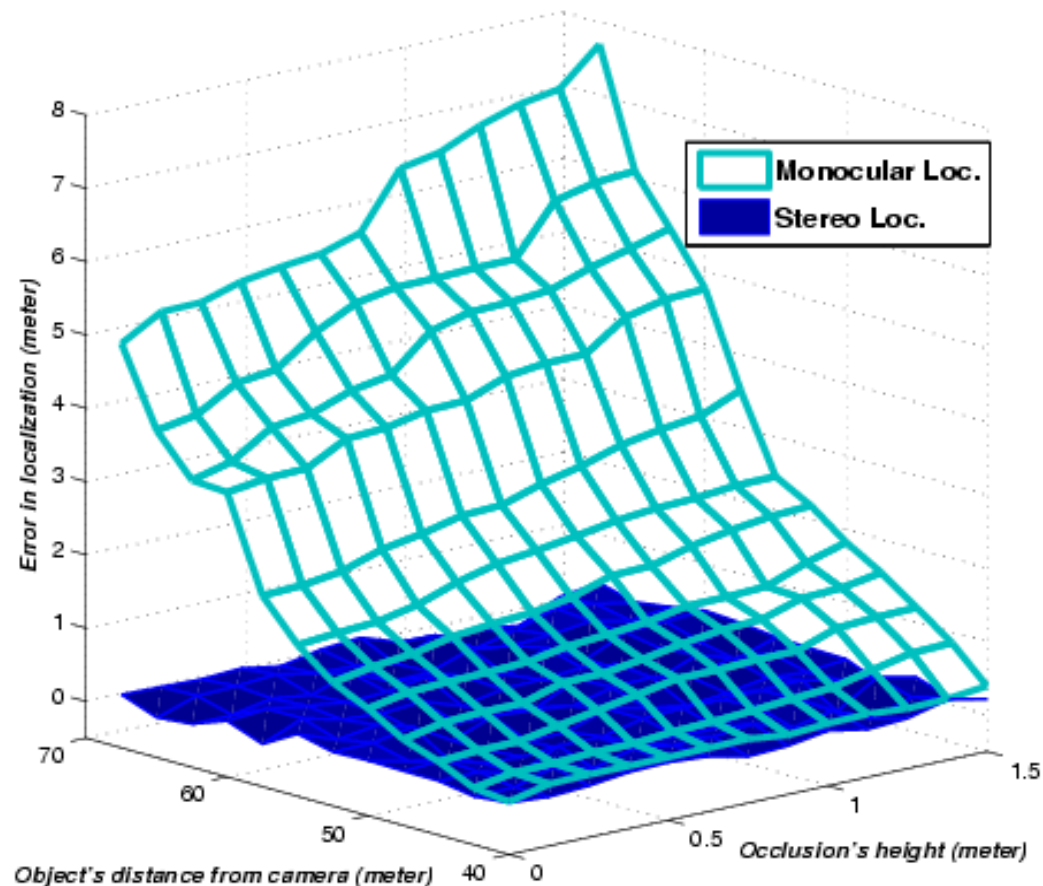
PTZ camera frames



Localization

- + Proposed stereo localization
- x Monocular localization

## Localization Error





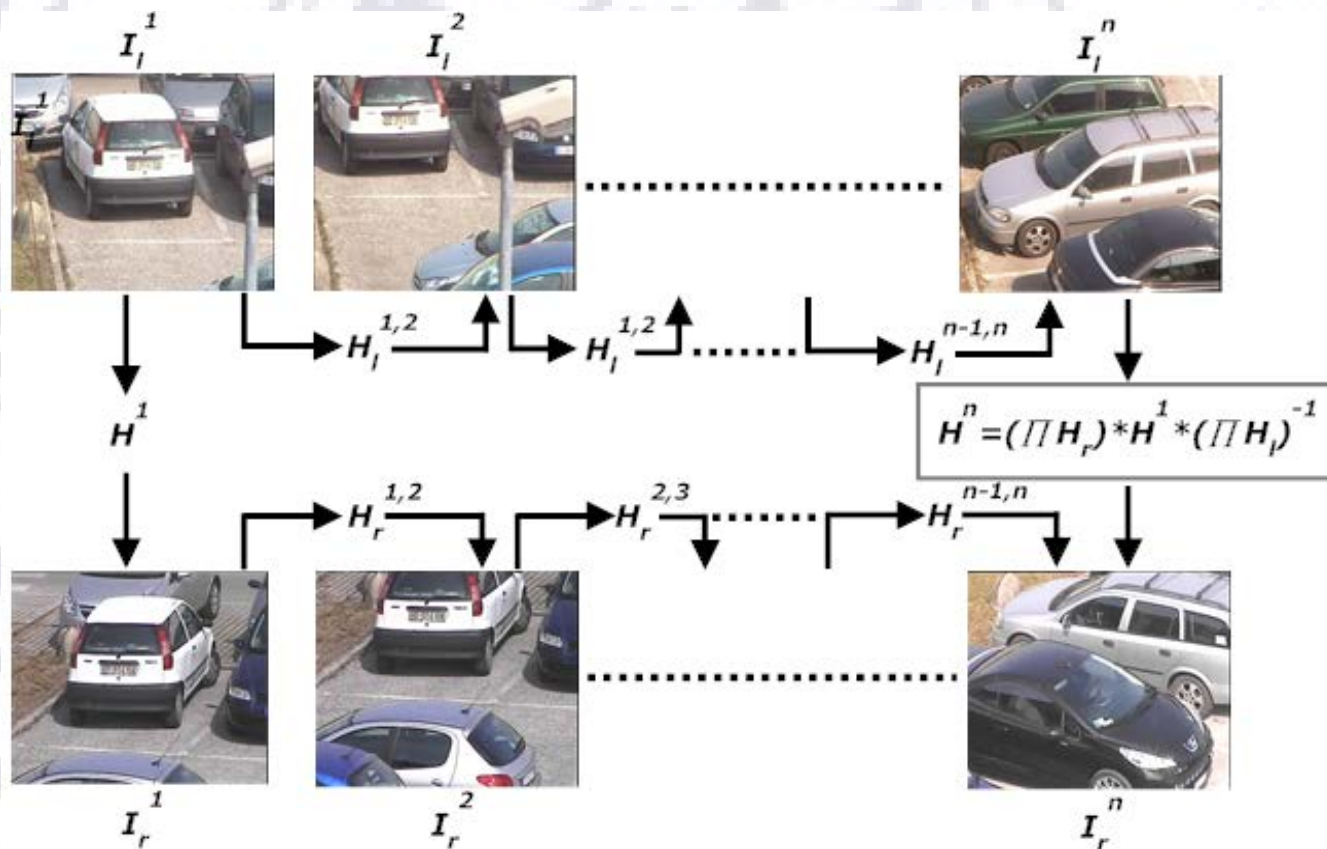
- Rectification is usually performed by using features:
  - Corners
  - Sift
  - Surf
- These features work well only under a slightly change in the point of view
- In stereo vision this means a short baseline

## Problem

**PTZs in a video network are deployed far away so they have a wide baseline**

## Solution for wide baseline matching

- Using the chain of homographies:





## OFFLINE OPERATIONS

- An offline LUT is constructed for the possible combinations of pan and tilt angles of both the cameras based on the sampling.
- A NN is trained to estimated homography parameters given the pan and tilt position.

## ONLINE OPERATIONS

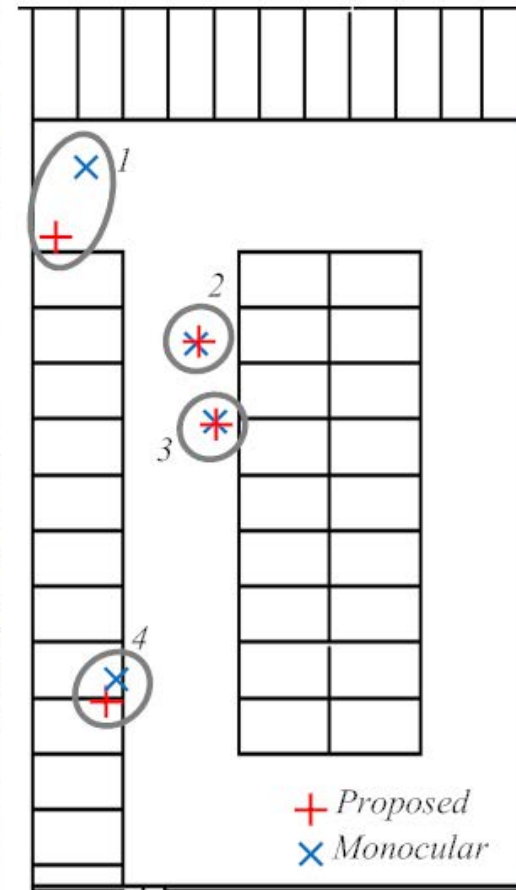
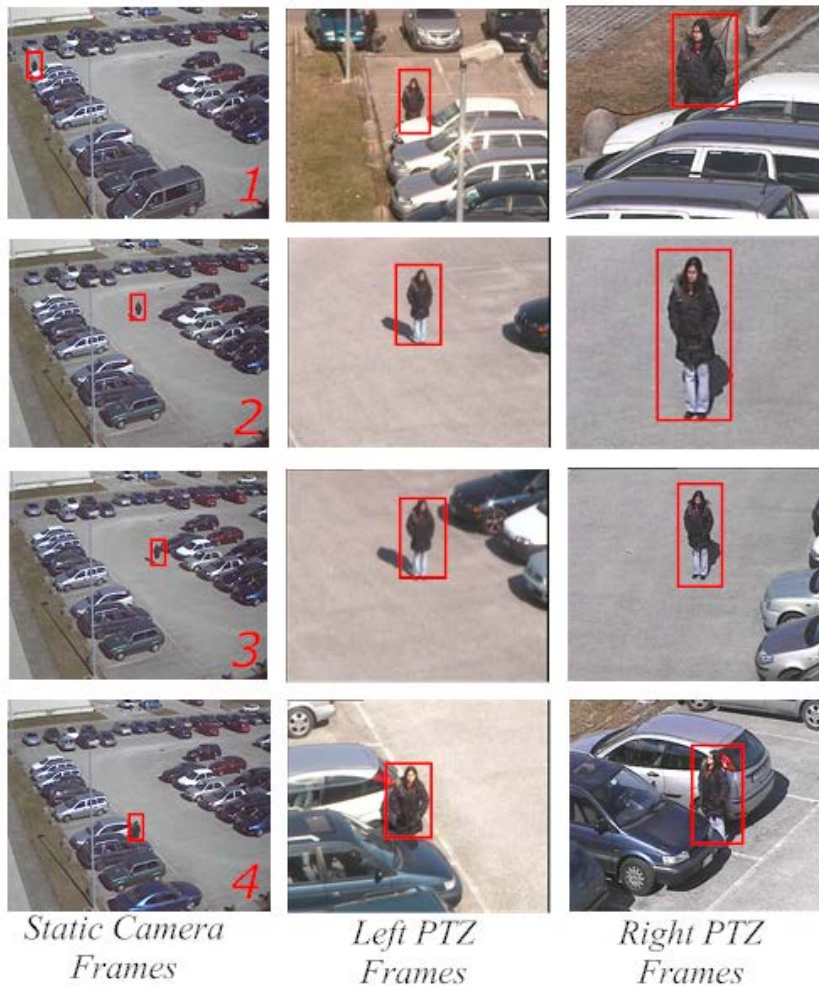
- Cameras redirected on the target
- Homography matrices are computed using NN interpolation
- Finally the target is localized by using its 3D position obtained by stereo vision.

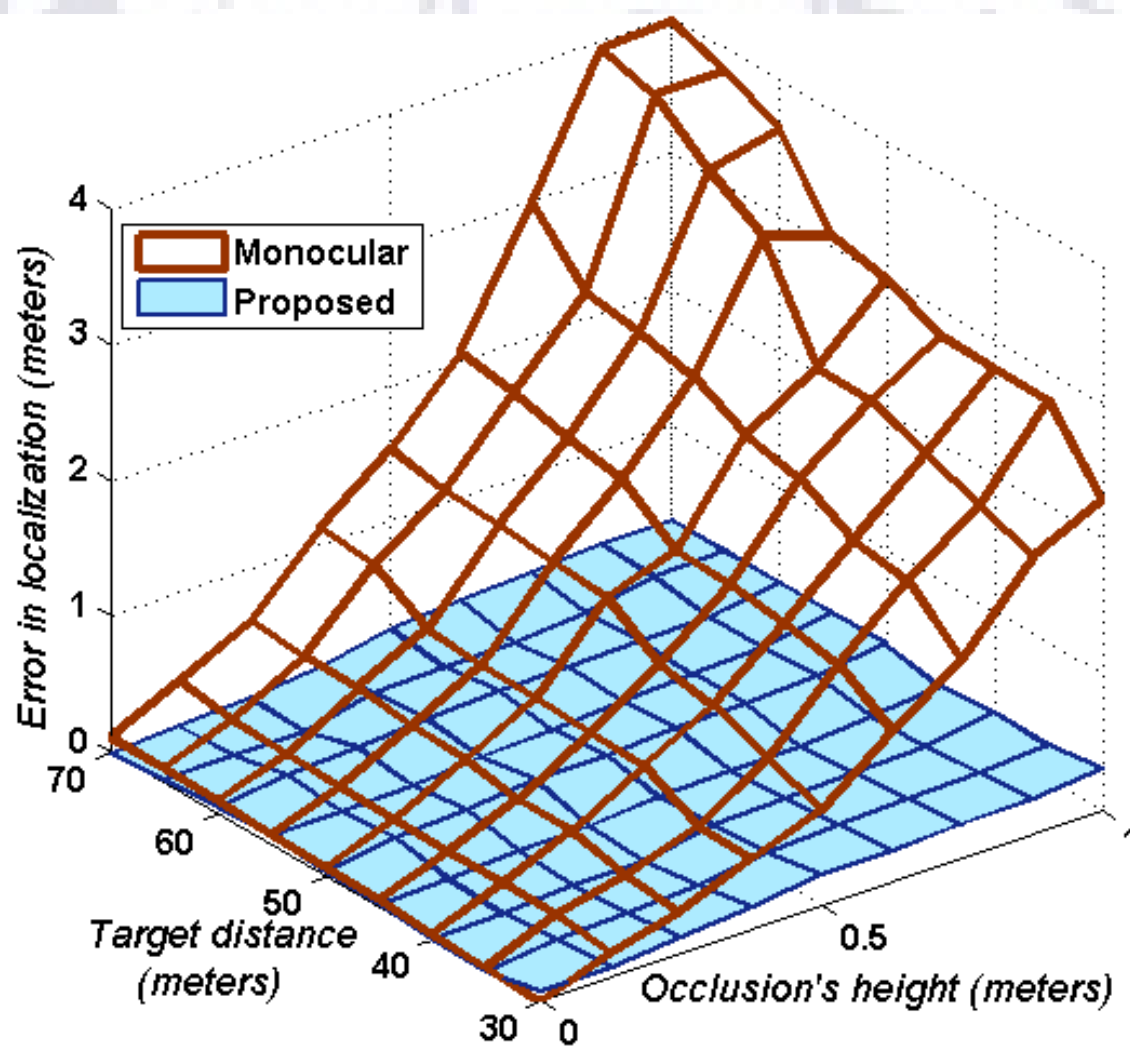


## Construction of LUT

- Sample the different pan and tilt angles for the whole pan and tilt ranges for the left and right PTZ camera into equal intervals.
- Compute the possible rectification transformations pairs for these image pairs of stereo images.
- Store all these pairs in a LUT where the indices are the Pan and Tilt angles of the two cameras and the related information is the rectification.

## results for localization







## Steps:

- Grab the sequences from both (static and PTZ) cameras.
- Rectify the corresponding stereo frames.
- Normalize the intensities in stereo frames using linear regression technique.
- Perform SSD measure for disparity estimation.

(Focal ratio: 1.0 (left) & 0.97 (right))



(a)



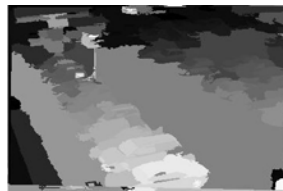
(b)



(c)



(d)



(e)

*Stereo pairs (a & b), rectified pairs (c & d)*

*Range-image (e)*



(a)



(b)



(c)



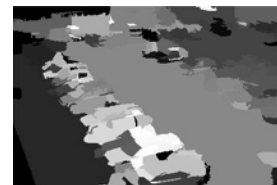
(d)



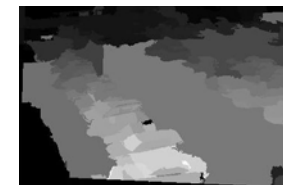
(e)



(f)



(g)



(h)

*Focal Ratio- 0.94 (left), 0.90 (right)*



(a)



(b)



(c)



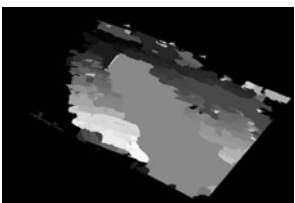
(d)



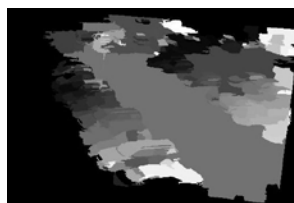
(e)



(f)



(g)



(h)



(a)



(b)



(c)



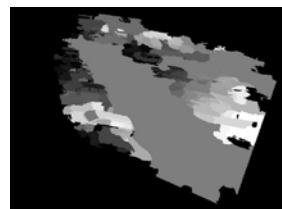
(d)



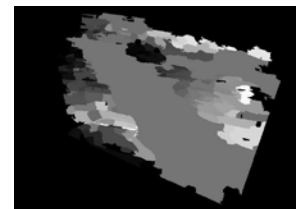
(e)



(f)



(g)



(h)



1. Abidi, B., Koschan, A., Kang, S., Mitckes, M., Abidi, M., 2003. Automatic Target Acquisition and Tracking with Cooperative Static and PTZ Video Cameras. Kluwer Academic, Ch. Multisensors Surveillance Systems: The Fusion, pp. 43–59.
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# How can the PTZs monitor better?

Optimization of the area coverage by  
selecting the PTZs fields of view



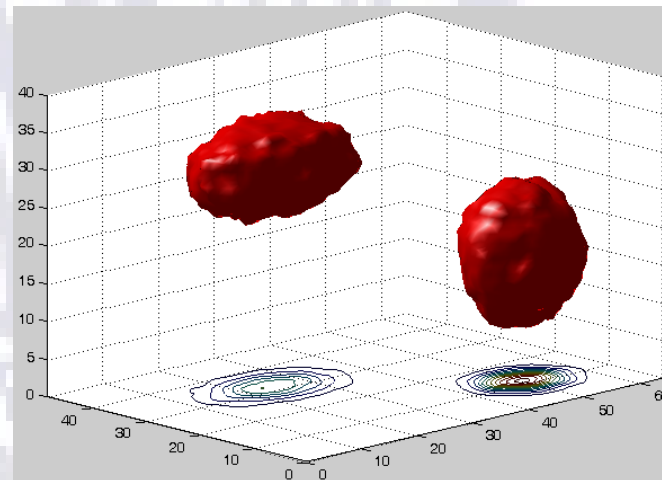
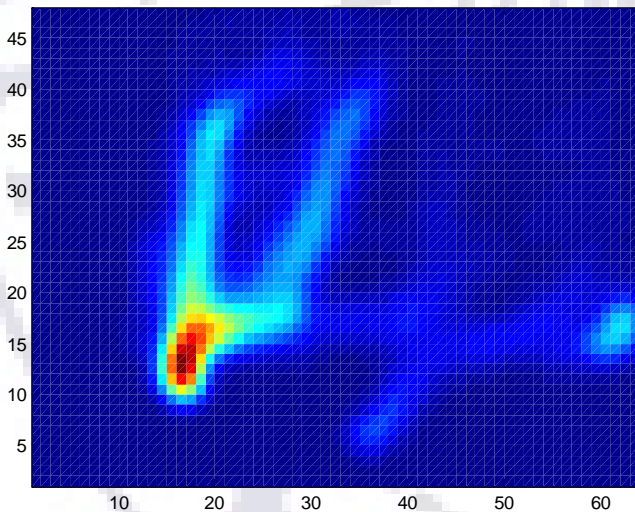


- Nowadays large camera networks are becoming more and more popular, e.g. for surveillance systems, traffic monitoring, etc.
- However, the performance of the system will be suboptimal if the cameras are observing the wrong zones
- How can we achieve an optimal coverage of the observed environment?



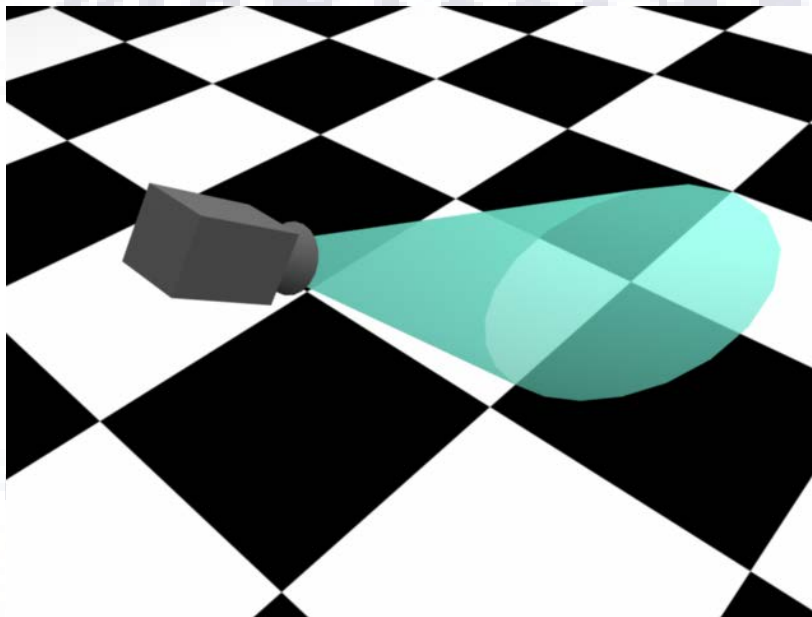
- A method for optimizing the configuration (pan, tilt and zoom values) of a network of PTZ cameras could be interesting

- Optimize the coverage of the observed area according to a *relevance map*, denoting which zones are more important than others
- The exact definition of the relevance maps depends on the specific application. Relevance maps can either be 2D or 3D



- Approximate the zone observed by a camera with a *cone of view*. The *observation function* denotes if a point  $x$  falls within the cone of view of a camera with configuration parameters  $\Theta$

$$\gamma_k(\mathbf{x}; \Theta) = \begin{cases} 1 & \text{if } \mathbf{x} \in \text{cone-of-view of camera } k \\ 0 & \text{otherwise} \end{cases}$$



- The score function measures the total coverage of a point  $\mathbf{x}$ , giving higher scores to points observed by more than one camera and to points with higher relevance

$$f(\mathbf{x}; \Theta, C) = \left( \sum_{k=1}^K c_k \gamma_k(\mathbf{x}; \Theta) \right)^{\omega(\mathbf{x})}$$

- The relevance of a point is given by a relevance map

$$w(\mathbf{x}) \geq 0 \quad \forall \mathbf{x} \in H$$

- Each camera receives an importance score

$$c_k \in C$$



- The global score function in case H is a discrete set of points:

$$\Lambda(\Theta, C) = \prod_{\mathbf{x} \in \mathcal{H}} f(\mathbf{x}; \Theta, C)$$

- The goal of the proposed method is to compute the unknowns  $\Theta$  (pan  $\phi$ , tilt  $\theta$ , cone of view width  $\zeta$ ) and  $C$  (camera weights) such that the global score function is maximized

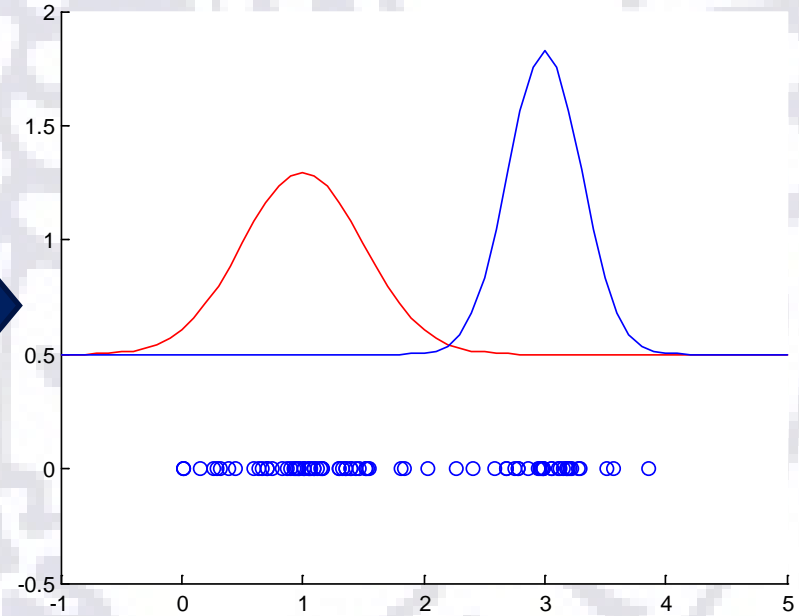
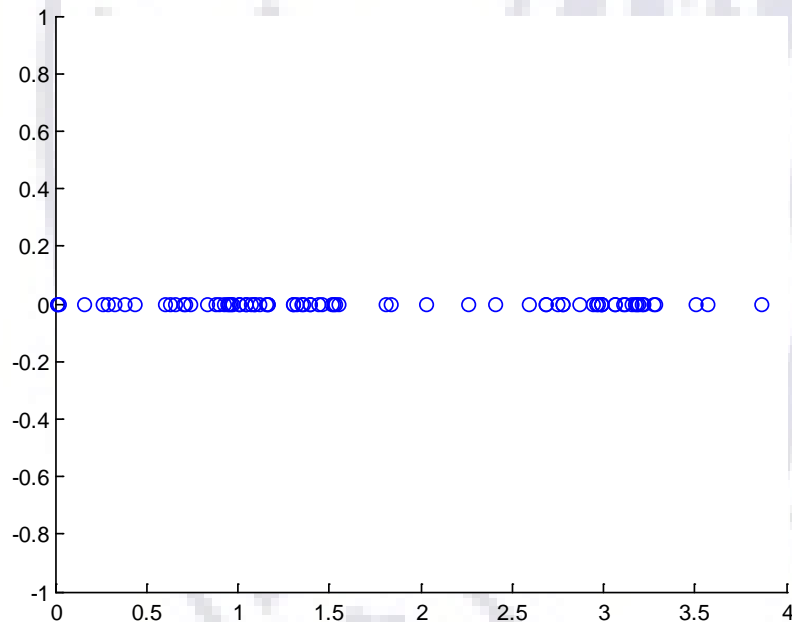
- The Expectation-Maximization algorithm finds a maximum likelihood estimate of the unobserved latent variables of a statistical model.
- A popular statistical model used with EM is the mixture of Gaussians:

$$p(x; \Theta) = \sum_{k=1}^K c_k G(x; \mu_k, \sigma_k)$$

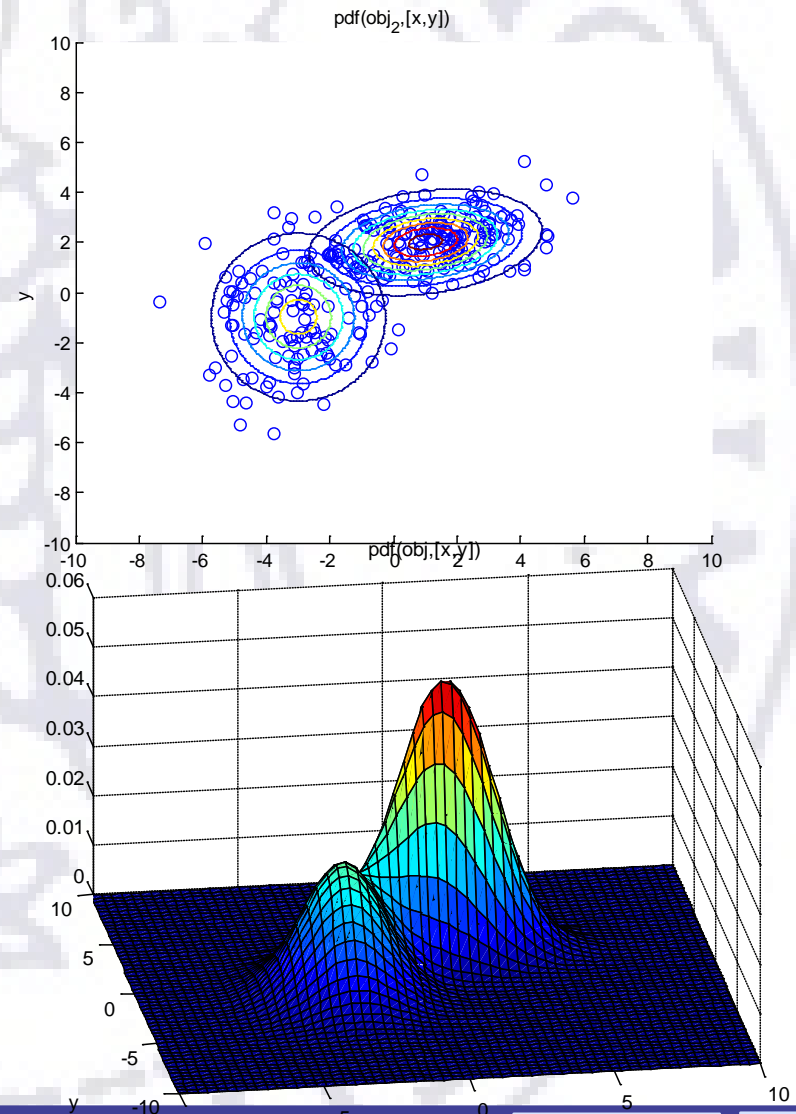
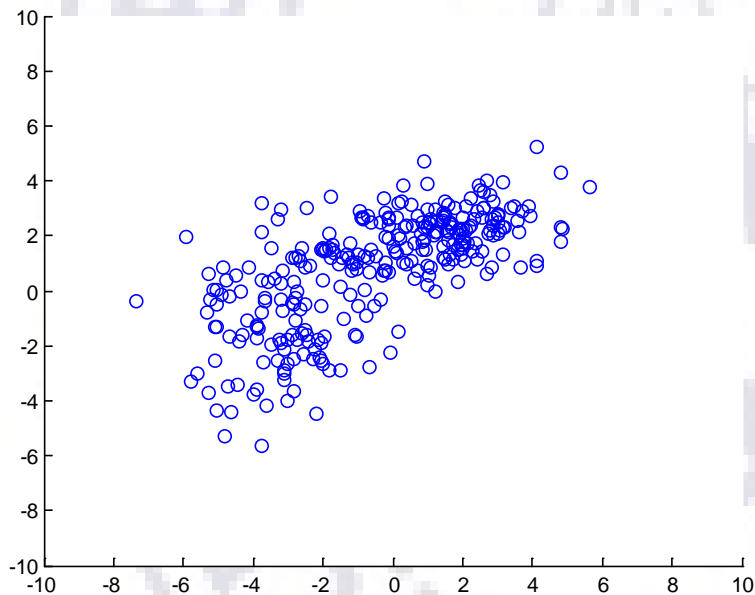
With  $G$  Gaussian function and  $\Theta = (c_1, \mu_1, \sigma_1, \dots, c_K, \mu_K, \sigma_K)$

$c_k$  are weights such that  $c_k \geq 0$ ,  $\sum_{k=1}^K c_k = 1$

- Given a set of values  $X = \{x_1, \dots, x_N\}$  EM thus searches for the parameters that better describe their distribution in terms of a Mixture-of-Gaussians model



- Also works with bivariate or multivariate Gaussian distributions:





- the likelihood is expressed as:

$$\Lambda(X, \Theta) = \prod_{n=1}^N p(x_n, \Theta)$$

In the case of mixture of Gaussians this becomes:

$$\Lambda(X, \Theta) = \prod_{n=1}^N \sum_{k=1}^K c_k G(x; \mu_k, \sigma_k)$$

and the log-likelihood is:

$$\lambda(X, \Theta) = \sum_{n=1}^N \log \sum_{k=1}^K c_k G(x; \mu_k, \sigma_k)$$

- Goal: find parameters  $\Theta$  that maximize the log-likelihood
- Solution: use the Lagrange multipliers method and set to zero the partial derivatives of  $\lambda(X, \Theta)$  with respect to each parameter  $\mu_k, \sigma_k, c_k$
- The solving equations, in the simplified case of mixture of isotropic bivariate Gaussian functions, are:

$$\bullet \quad \mu_k = \frac{\sum_{n=1}^N p(k|n) x_n}{\sum_{n=1}^N p(k|n)}$$

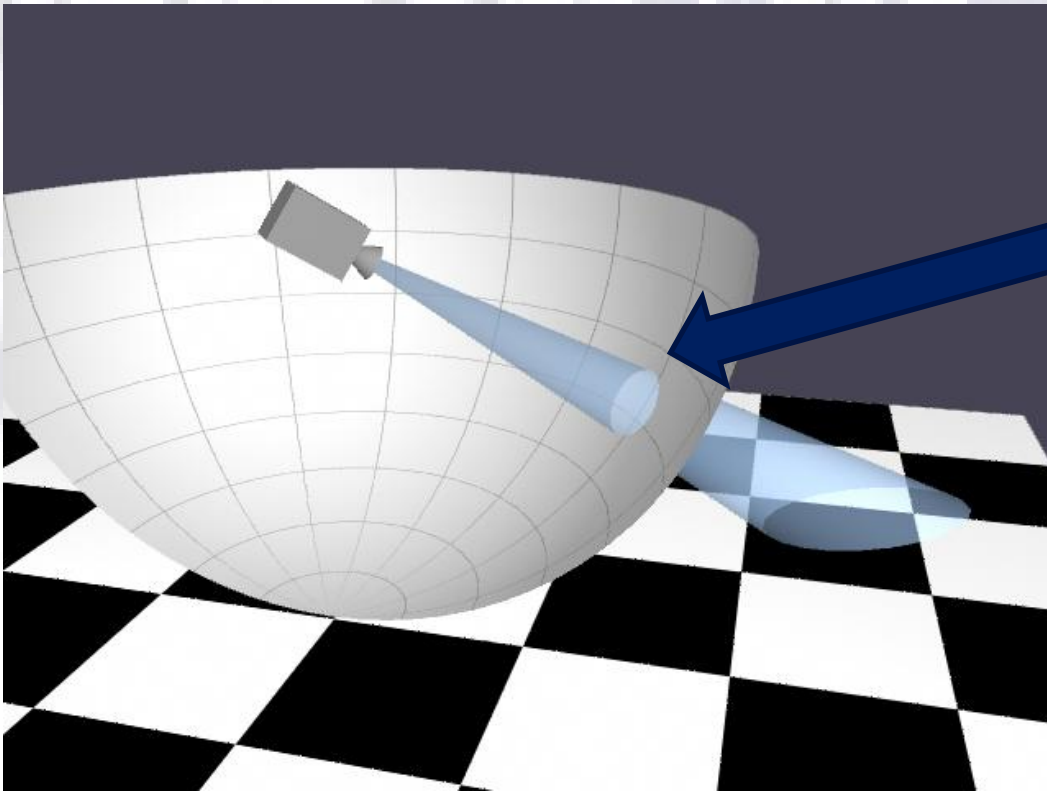
$$\bullet \quad \sigma_k^2 = \frac{\sum_{n=1}^N p(k|n) \|x_n - \mu_k\|^2}{2 \sum_{n=1}^N p(k|n)}$$

$$\bullet \quad c_k = \frac{1}{N} \sum_{n=1}^N p(k|n)$$

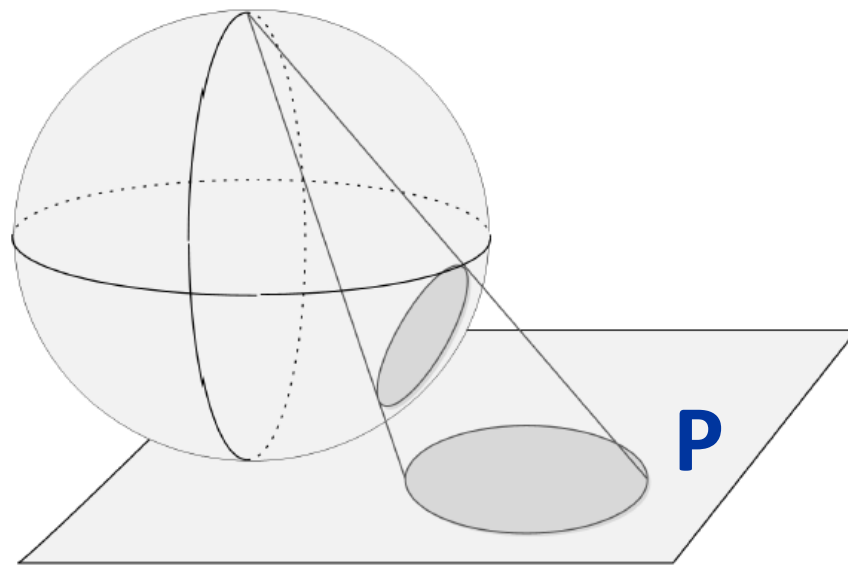
$$p(k|n) = \frac{c_k G(x_n; \mu_k, \sigma_k)}{\sum_{z=1}^K c_z G(x_n; \mu_z, \sigma_z)}$$

mutually dependent,  
iterate until convergence

- The observation function  $\gamma_k$  does not depend to the distance of point  $x$  from the camera. Thus, we can drop a dimension and project all the observed points on the surface of a sphere centered on the camera.



Each point can now be described with two angular coordinates. The observed region collapses on a circle on the surface of the sphere.



The circles can be projected on a plane P using a stereographic projection, a circle-preserving projection widely used in cartography.

$$\begin{cases} \phi_k = \arctan\left(\frac{y-Y_k}{x-X_k}\right) \\ \theta_k = \arctan\left(\frac{\sqrt{(x-X_k)^2 + (y-Y_k)^2}}{z-Z_k}\right) \end{cases}$$

angles

$$\begin{cases} u_k = 2 \tan(\theta_k/2) \cos \phi_k \\ v_k = 2 \tan(\theta_k/2) \sin \phi_k \end{cases}$$

coordinates in P

- The equivalent of the observation function on the plane P is thus a circle:

$$\Gamma_k(u, v; \Theta) = \begin{cases} 1 & \text{if } (u - \mu_{u,k}^\Theta)^2 + (v - \mu_{v,k}^\Theta)^2 \leq (\sigma_k^\Theta)^2 \\ 0 & \text{otherwise} \end{cases}$$

- We now approximate this circle with a bivariate, isotropic Gaussian function. This approximation helps keeping the optimization problem tractable and intuitively gives more importance to central parts of the image

$$\Gamma_k(\mathbf{x}; \Theta) \approx G_k(\mathbf{x}; \Theta) = \frac{1}{2\pi\sigma_k^{\Theta^2}} e^{-\frac{\|\mathbf{x} - \mu_k^\Theta\|^2}{2\sigma_k^{\Theta^2}}}$$



- If  $M(\mathbf{x})$  is the stereographic projection of point  $\mathbf{x}$  on the plane  $P$ , the score function can now be rewritten as

$$f(\mathbf{x}; \Theta, C) = \left( \sum_{k=1}^K c_k G_k(M_k(\mathbf{x}); \Theta) \right)^{\omega(\mathbf{x})}$$

- This leads to a new global score function to be maximized, whose logarithm is:

$$\lambda(\Theta, C) = \sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x}) \log \sum_{k=1}^K c_k G_k(M_k(\mathbf{x}); \Theta)$$



The final solving equations (to be iterated until convergence) are:

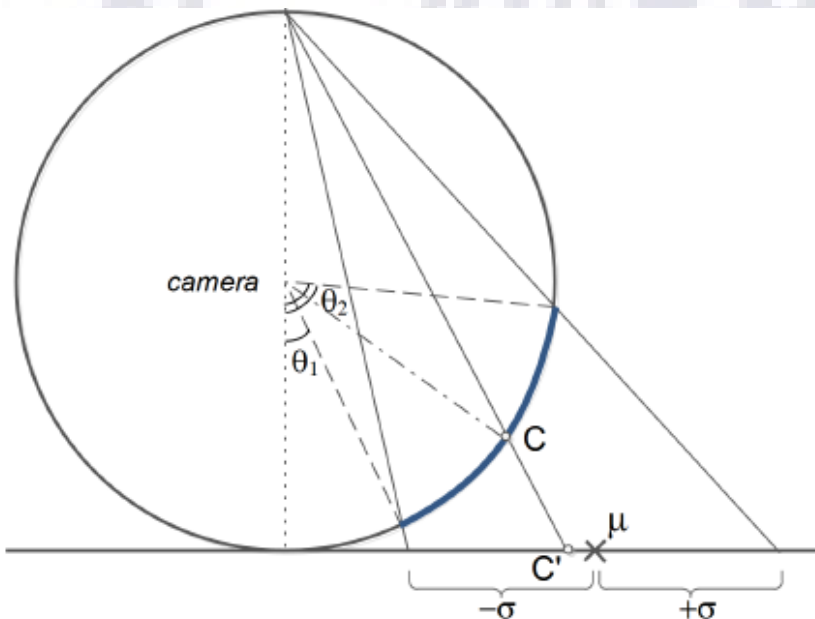
$$\begin{aligned}\mu_k^\Theta &= \frac{\sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x}) p(k|\mathbf{x}) M_k(\mathbf{x})}{\sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x}) p(k|\mathbf{x})} \\ \sigma_k^{\Theta^2} &= \frac{\sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x}) p(k|\mathbf{x}) \|M_k(\mathbf{x}) - \mu_k^\Theta\|^2}{2 \sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x}) p(k|\mathbf{x})} \\ c_k &= \frac{\sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x}) p(k|\mathbf{x})}{\sum_{\mathbf{x} \in \mathcal{H}} \omega(\mathbf{x})}\end{aligned}$$

Maximization equations

$$p(k|\mathbf{x}) = \frac{c_k \omega(\mathbf{x}) G(M_k(\mathbf{x}); \Theta)}{\sum_{z=1}^K c_z \omega(\mathbf{x}) G(M_z(\mathbf{x}); \Theta)}$$

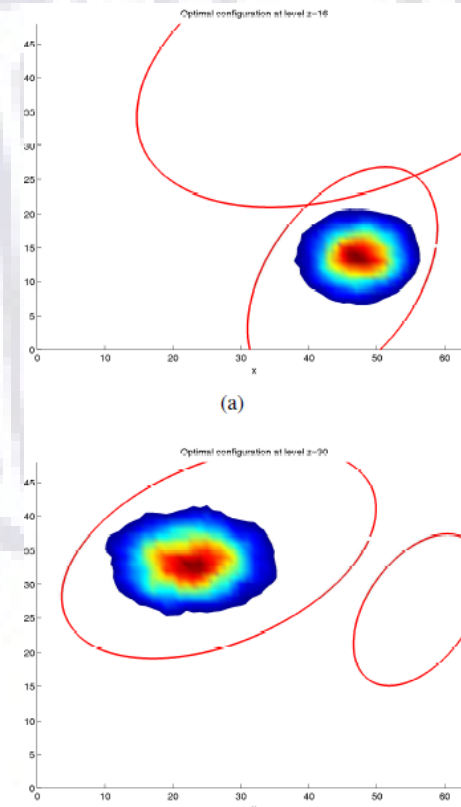
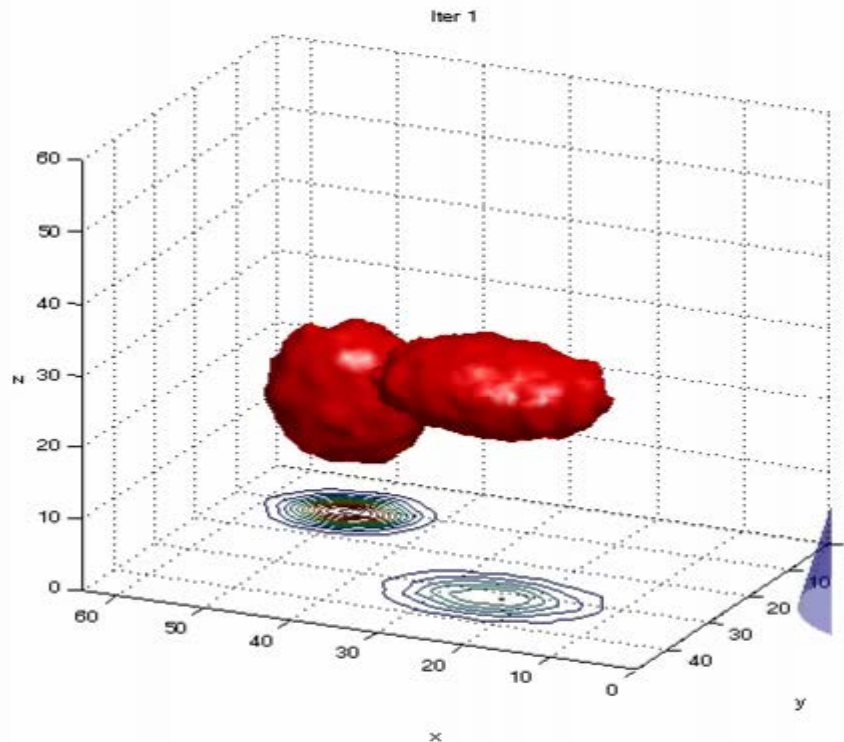
Expectation equation

- The results on plane P (in terms of centers and variances of the Gaussian functions) can be projected back using an inverse stereographic projection, in order to obtain the pan, tilt and zoom angles of each camera.
- Note: we cannot simply back-project the center  $\mu$  of each Gaussian function, as centers are not preserved by stereographic projections.
  - The problem can be solved by first computing the two  $\theta_1, \theta_2$  angles



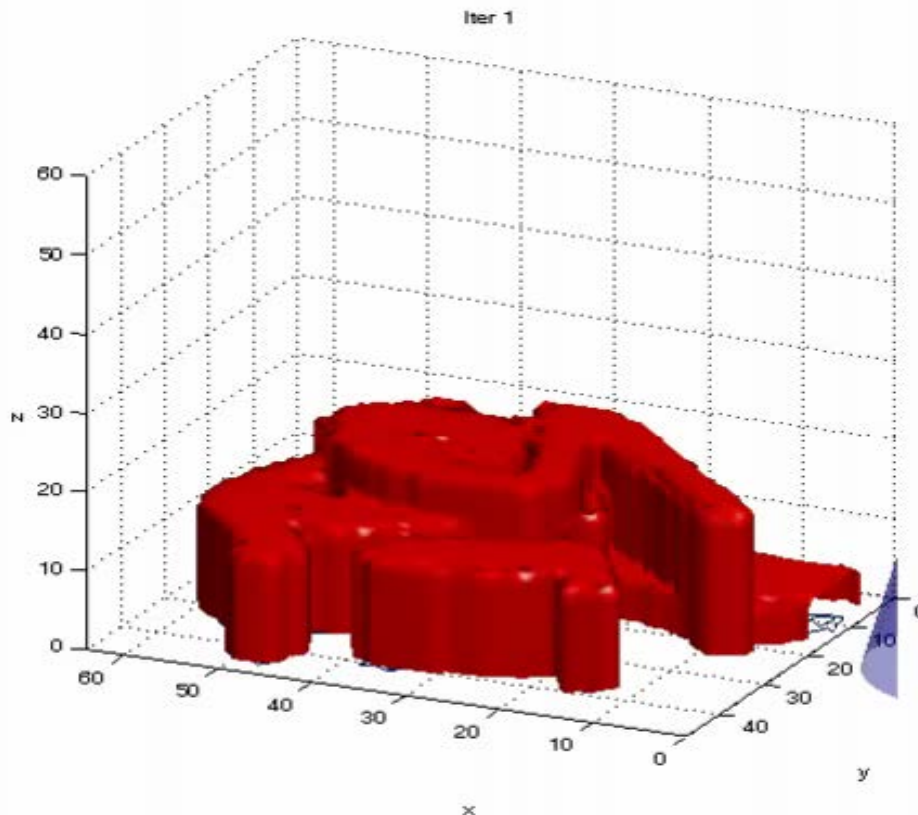
$$\begin{cases} \theta_1 &= 2 \arctan \left( \frac{\|\mu_k\| + \sigma_k}{2} \right) \\ \theta_2 &= 2 \arctan \left( \frac{\|\mu_k\| - \sigma_k}{2} \right) \\ \phi_k &= \arctan (\mu_{v,k} / \mu_{u,k}) \\ \theta_k &= (\theta_1 + \theta_2) / 2 \\ \zeta_k &= (\theta_1 - \theta_2) / 2 \end{cases}$$

- A simple example where the relevance map is a mixture of two Gaussian trivariate functions. The red surface is the isosurface of relevance  $w=0.1$

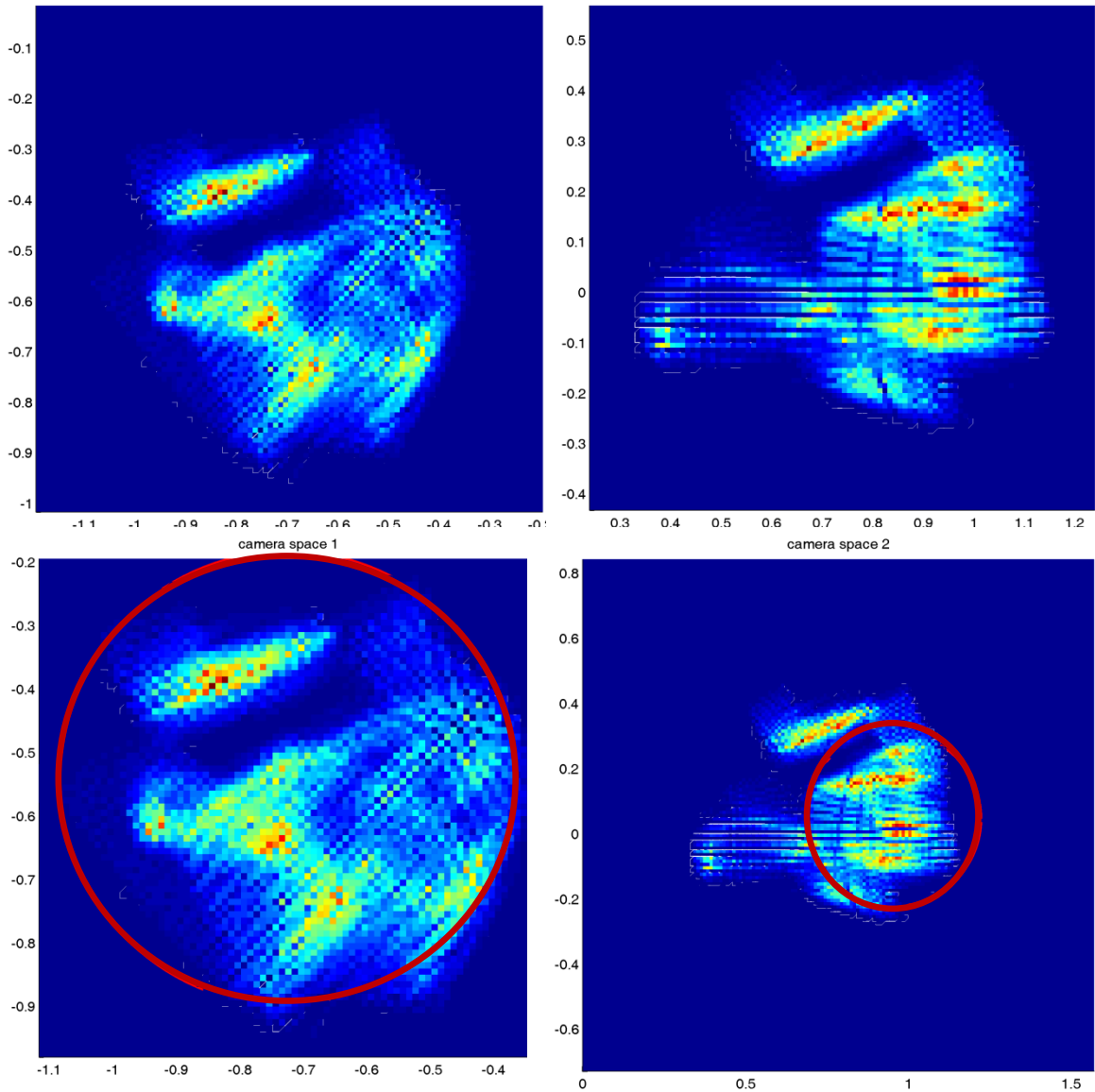


Final results at heights 16 and 30

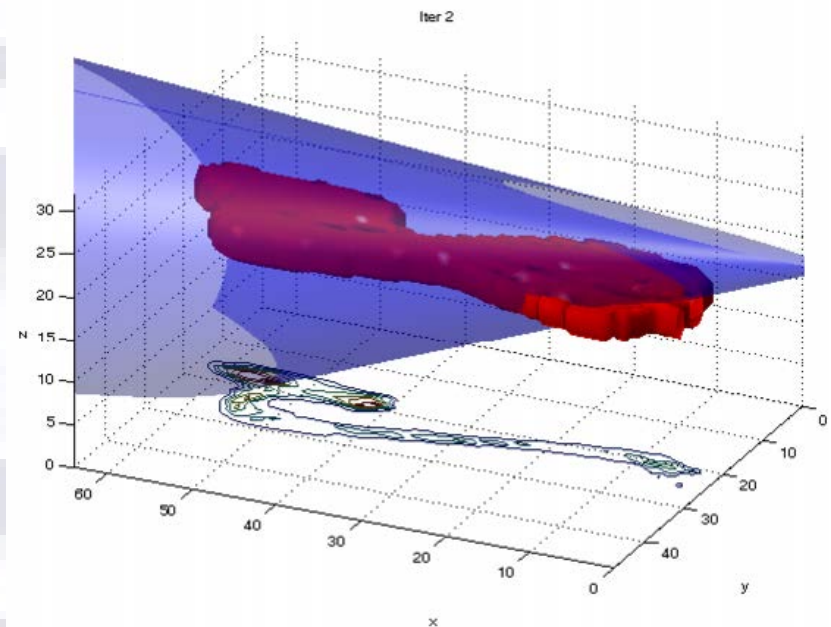
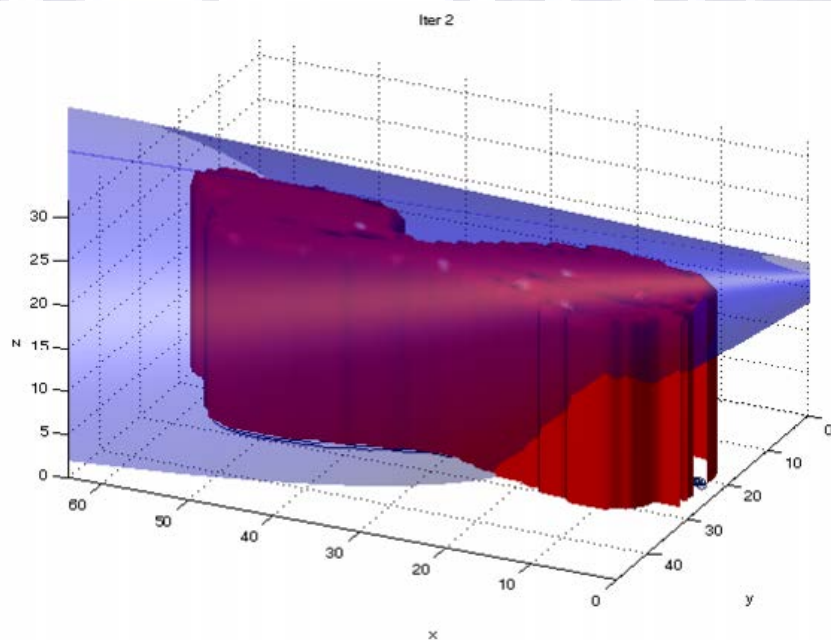
- In this example the relevance map denotes the 3D location of moving objects accumulated over a long period of time



- Relevance Maps computed for the cameras positions
- Coverage achieved by the two cameras

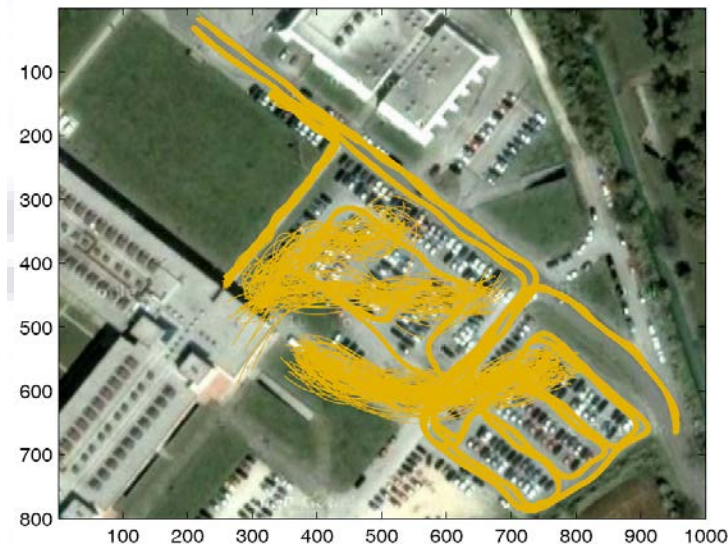


- 3D maps can help focusing only on specific regions. The data below are obtained mapping the 3D volume occupied by a moving person. If we consider only the upper region the camera can be more effectively focused on the head of the person.



- In order to give a measurable performance parameter, the concept of *total coverage* can be adopted, defined as the ratio among the relevance of all the considered points covered by at least one camera and the total relevance.
- EM achieve a total coverage 93%

dataset	total coverage	dataset	total coverage
1	0.9693	11	0.9987
2	0.9998	12	0.9545
3	0.9723	13	0.9785
4	0.9923	14	0.9614
5	0.9977	15	0.9735
6	0.9824	16	0.9788
7	0.9775	17	0.9817
8	0.9891	18	0.9937
9	0.9815	19	0.9798
10	0.9304	20	0.9615





- Activities can be detected and exploited to compute related 3D relevance maps.
- Relevance maps are projected in a space where the execution of EM algorithm is easier and more efficient.
- The reconfiguration algorithm optimally computes the best camera parameters to best cover the monitored area considering the activities occurring in it.
- A subspace of the 3D environment can be selected to focus the reconfiguration on desired tasks or objects' parts.